



basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

**SENIOR CERTIFICATE EXAMINATIONS/
NATIONAL SENIOR CERTIFICATE EXAMINATIONS**

MATHEMATICS P2

MAY/JUNE 2023

MARKS: 150

TIME: 3 hours

Stanmorephysics

This question paper consists of 13 pages and 1 information sheet.



INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

1. This question paper consists of 10 questions.
2. Answer ALL the questions in the SPECIAL ANSWER BOOK provided.
3. Clearly show ALL calculations, diagrams, graphs, etc. which you have used in determining your answers.
4. Answers only will NOT necessarily be awarded full marks.
5. You may use an approved scientific calculator (non-programmable and non-graphical), unless stated otherwise.
6. If necessary, round off answers correct to TWO decimal places, unless stated otherwise.
7. Diagrams are NOT necessarily drawn to scale.
8. An information sheet with formulae is included at the end of the question paper.
9. Write neatly and legibly.



QUESTION 1

- 1.1 The owner of a small company wishes to establish whether advertising in a regional newspaper is effective. The table below shows the amount spent on advertising and the corresponding sales figures for the last 9 years.

Amount spent on advertising (in rands) (x)	21 300	23 700	24 800	30 540	24 100	40 680	22 400	35 250	29 110
Sales (in rands) (y)	311 500	326 700	349 200	470 000	316 100	564 200	314 000	487 300	392 900

- 1.1.1 Determine the equation of the least squares regression line for the data. (3)
- 1.1.2 Predict the sales for a year in which the company will spend R28 500 on advertising. (2)
- 1.1.3 Write down the correlation coefficient of the data. (1)
- 1.1.4 Describe the association between the amount spent on advertising in the regional newspaper and the sales of this company. (1)
- 1.2 The profit that the small company made over the same 9 years is given in the table below.

Profit (in rands)	110 750	107 376	152 338	244 480	144 021	275 994	121 900	207 636	187 700
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- 1.2.1 Calculate the mean profit made over the 9 years. (2)
- 1.2.2 Write down the standard deviation for the data. (1)
- 1.2.3 Determine the number of years in which the company made a profit that was greater than one standard deviation above the mean. (2)

[12]



QUESTION 2

The ages of the people who attended a music concert was summarised in the table below.



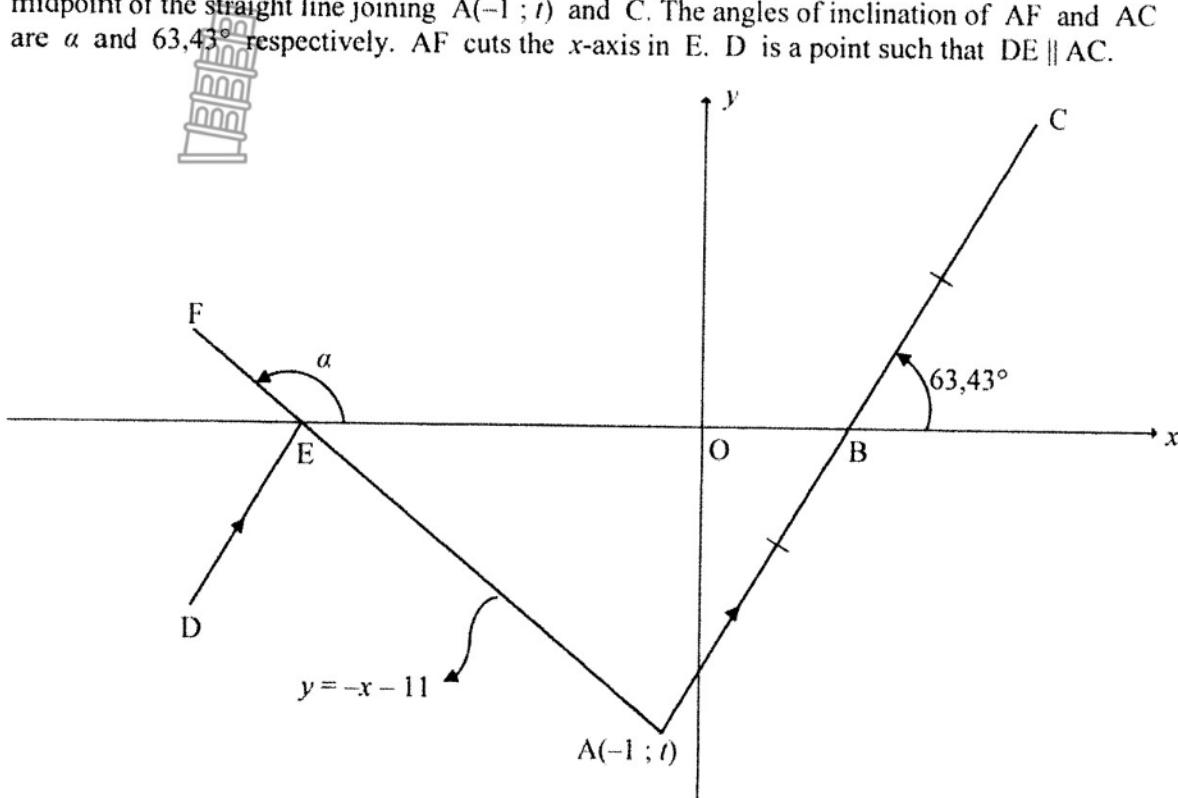
AGE	NUMBER OF PEOPLE
$5 < x \leq 15$	20
$15 < x \leq 25$	25
$25 < x \leq 35$	60
$35 < x \leq 45$	90
$45 < x \leq 55$	55
$55 < x \leq 65$	40
$65 < x \leq 75$	30

- 2.1 Write down the modal class of the data. (1)
- 2.2 How many people attended the music concert? (1)
- 2.3 On the grid provided in the ANSWER BOOK, draw a cumulative frequency graph (ogive) to represent the above data. (4)
- 2.4 Use the cumulative frequency graph to determine the median age of the people who attended the music concert. (2)
[8]



QUESTION 3

In the diagram, the equation of line AF is $y = -x - 11$. B, a point on the x -axis, is the midpoint of the straight line joining A($-1 ; t$) and C. The angles of inclination of AF and AC are α and $63,43^\circ$ respectively. AF cuts the x -axis in E. D is a point such that $DE \parallel AC$.



3.1 Calculate the:

3.1.1 Value of t (2)

3.1.2 Size of α (2)

3.1.3 Gradient of AC, to the nearest whole number (2)

3.2 Determine the equation of AC in the form $y = mx + k$. (2)

3.3 Calculate the:

3.3.1 Coordinates of C (3)

3.3.2 Size of \hat{FED} (3)

3.4 G is a point such that EAGC, in that order, is a parallelogram.



Determine the equation of a circle centred at G and passing through the point B.

Write your answer in the form $(x - a)^2 + (y - b)^2 = r^2$.

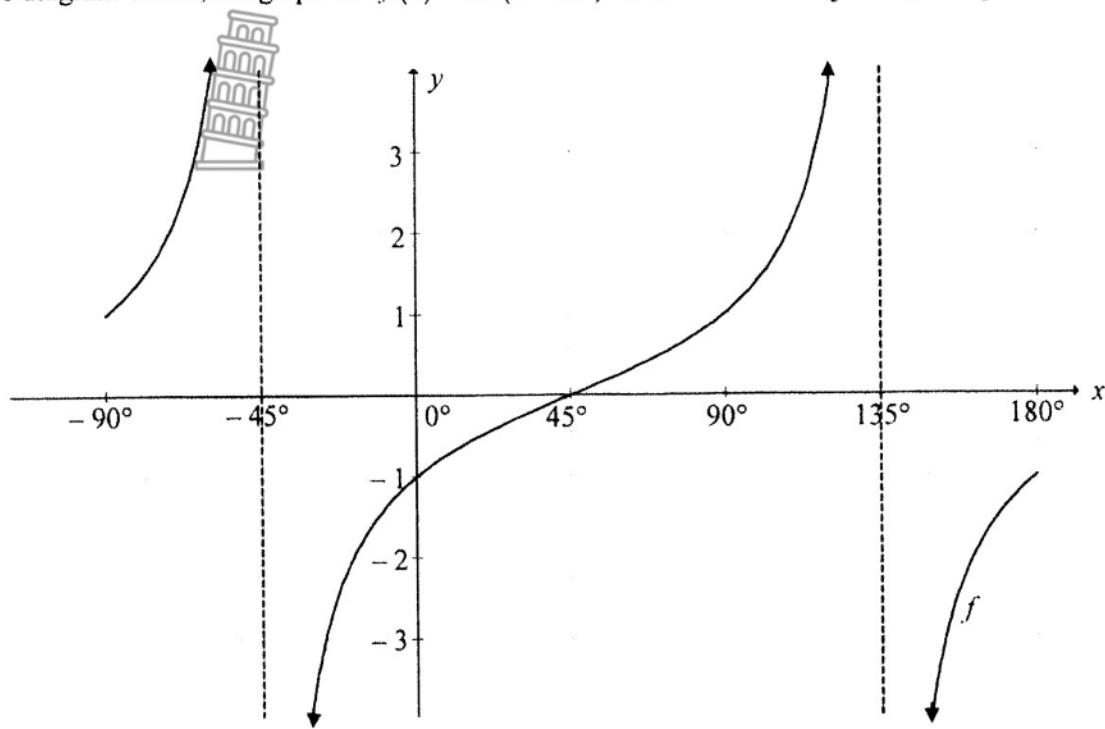
(4)

[18]



QUESTION 6

In the diagram below, the graph of $f(x) = \tan(x - 45^\circ)$ is drawn for $x \in [-90^\circ ; 180^\circ]$.



- 6.1 Write down the period of f . (1)
- 6.2 Draw the graph of $g(x) = -\cos 2x$ for the interval $x \in [-90^\circ ; 180^\circ]$ on the grid given in the ANSWER BOOK. Show ALL intercepts with the axes, as well as the minimum and maximum points of the graph. (3)
- 6.3 Write down the range of g . (1)
- 6.4 The graph of g is shifted 45° to the left to form the graph of h . Determine the equation of h in its simplest form. (2)
- 6.5 Use the graph(s) to determine the values of x in the interval $x \in [-90^\circ ; 90^\circ]$ for which:
 - 6.5.1 $f(x) > 1$ (2)
 - 6.5.2 $2\cos 2x - 1 > 0$ (4)



(2)

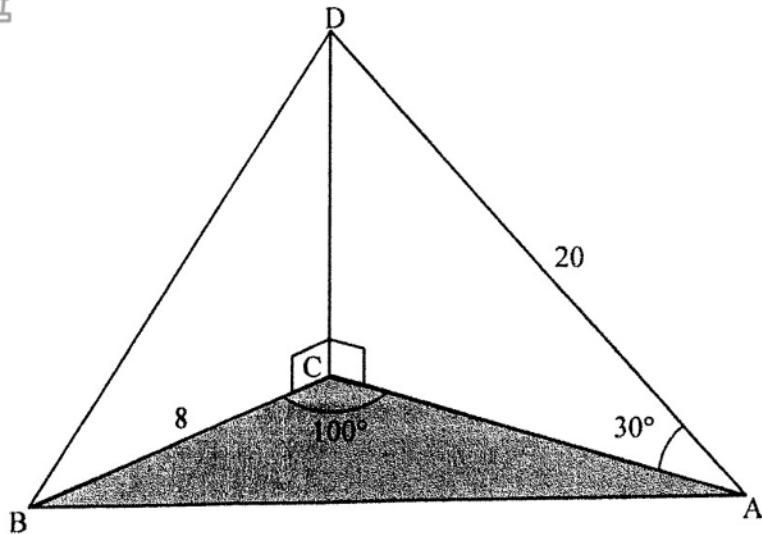
(4)

[13]



QUESTION 7

In the diagram, A, B and C are points in the same horizontal plane. D is a point directly above C, that is $DC \perp AC$ and $DC \perp BC$. It is given that $\hat{ACB} = 100^\circ$, $\hat{CAD} = 30^\circ$, $AD = 20$ units and $BC = 8$ units.



7.1 Calculate the length of:

7.1.1 AC (2)

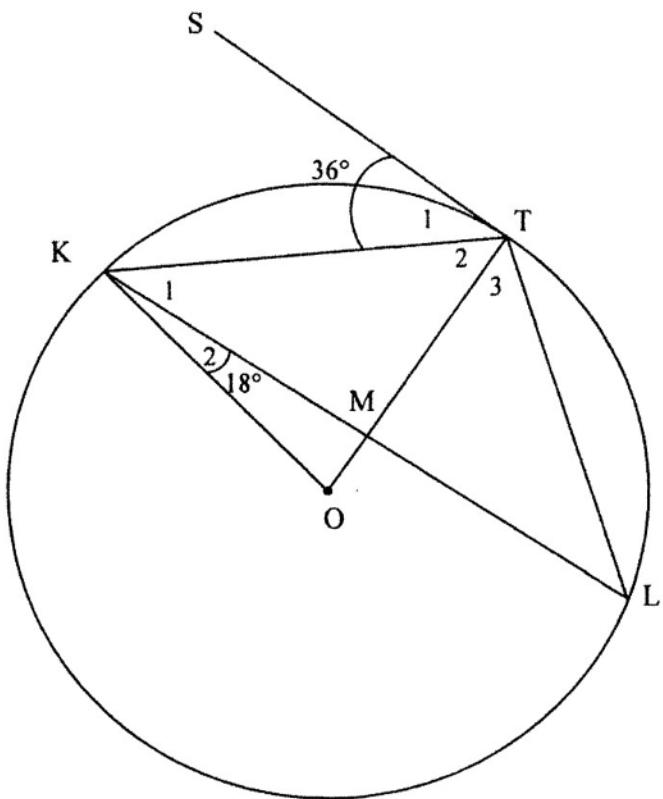
7.1.2 AB (3)

7.2 If it is further given that $\hat{ABD} = 73,4^\circ$, calculate the size of \hat{ADB} . (3)
[8]



QUESTION 8

- 8.1 In the diagram, O is the centre of the circle. K, T and L are points on the circle. KT, TL, KL, OK and OT are drawn. OT intersects KL at M. ST is a tangent to the circle at T. $\hat{S}TK = 36^\circ$ and $\hat{OKL} = 18^\circ$.



- 8.1.1 Determine, giving reasons, the size of:

(a) \hat{T}_2 (2)

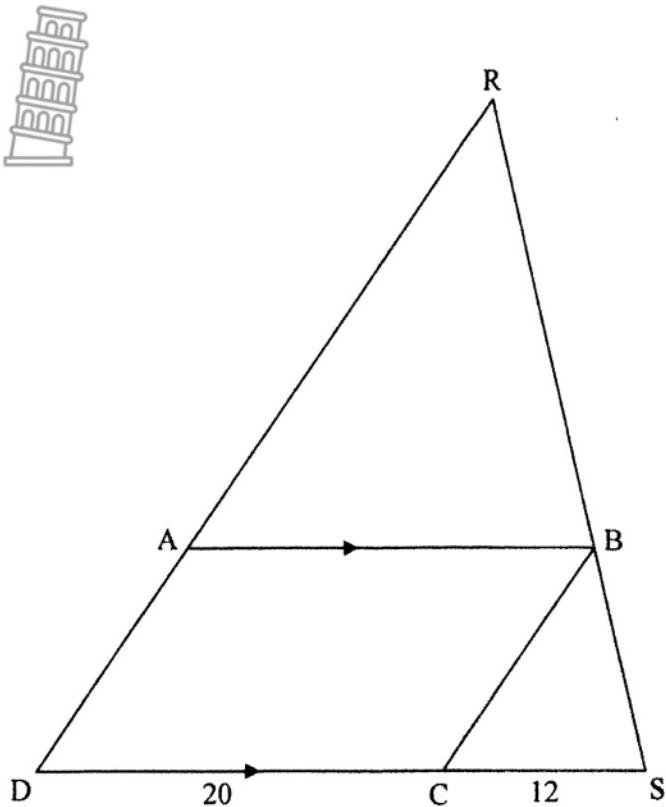
(b) \hat{L} (2)

(c) \hat{KOT} (2)

- 8.1.2 Prove, giving reasons, that $KM = ML$. (3)



- 8.2 In the diagram, $\triangle RDS$ is drawn. A, B and C are points on RD, RS and DS respectively such that $AB \parallel DS$ and $RB : BS = 5 : 3$. $DC = 20$ units and $CS = 12$ units.



8.2.1 Prove, giving reasons, that $BC \parallel AD$. (3)

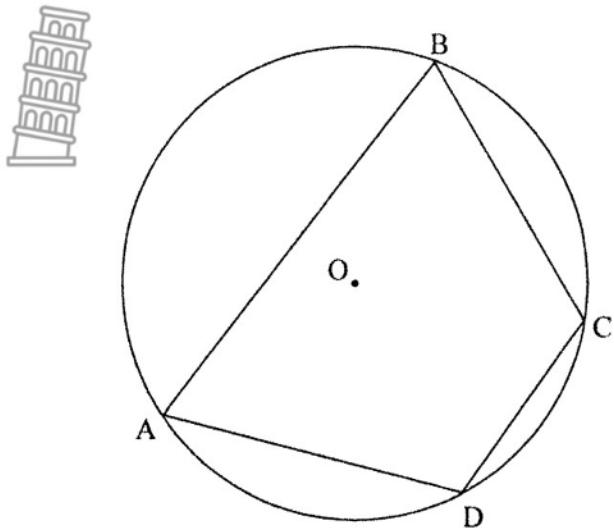
8.2.2 If it is further given that $RD = 48$ units, calculate, giving reasons, the value of the ratio $AD : AB$.

(3)
[15]



QUESTION 9

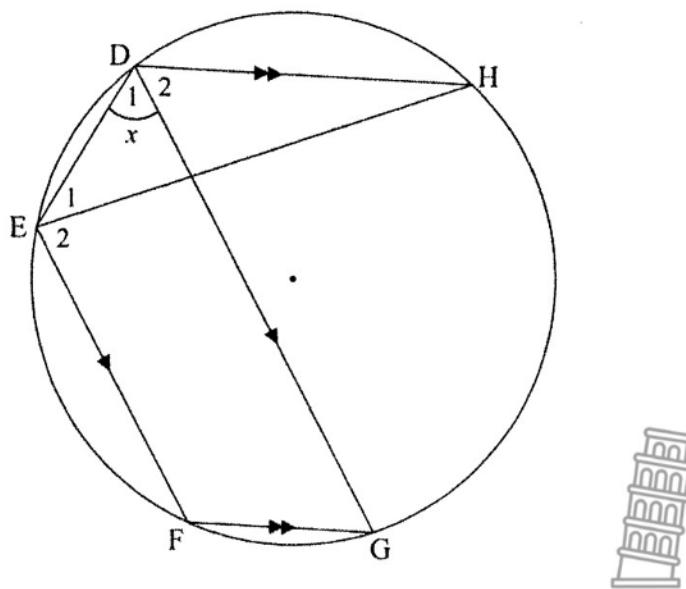
- 9.1 In the diagram, O is the centre of the circle. ABCD is a cyclic quadrilateral.



Use the diagram in the ANSWER BOOK to prove the theorem which states that the opposite angles of a cyclic quadrilateral are supplementary, that is prove that $\hat{B} + \hat{D} = 180^\circ$.

(5)

- 9.2 In the diagram, DEFG is a cyclic quadrilateral such that $EF \parallel DG$. H is another point on the circle such that $DH \parallel FG$. Chord EH is drawn. Let $\hat{D}_1 = x$.



Prove, giving reasons, that $\hat{D}_1 = \hat{D}_2$.

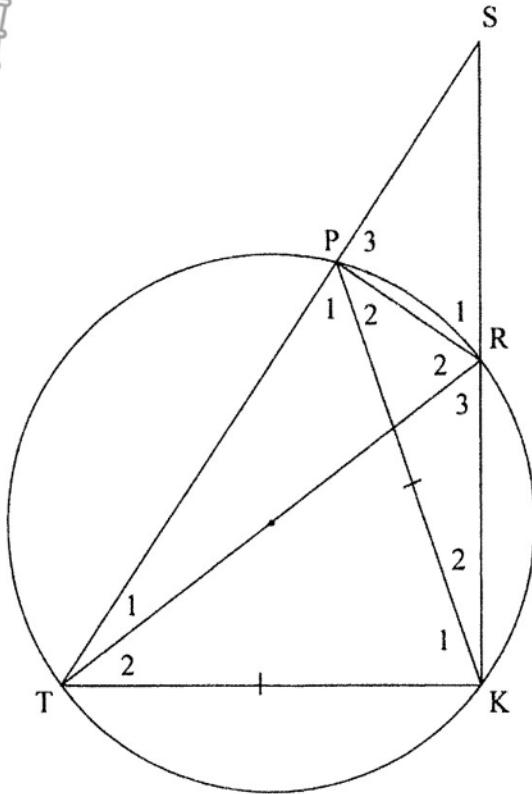
(4)

[9]



QUESTION 10

In the diagram, \overline{TR} is a diameter of the circle. PRKT is a cyclic quadrilateral. Chords \overline{TP} and \overline{KR} are produced to intersect at S . Chord \overline{PK} is drawn such that $PK = TK$.



- 10.1 Prove, giving reasons, that:

 - 10.1.1 SR is a diameter of a circle passing through points S, P and R (4)
 - 10.1.2 $\hat{S} = \hat{P}_2$ (5)
 - 10.1.3 $\Delta SPK \parallel\!\!\!|| \Delta PRK$ (3)

10.2 If it is further given that $SR = RK$, prove that $ST = \sqrt{6}RK$. (5)

[17]



TOTAL: 150



INFORMATION SHEET

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$A = P(1 + ni)$$



$$A = P(1 - ni)$$

$$A = P(1 - i)^n$$

$$A = P(1 + i)^n$$

$$T_n = a + (n - 1)d$$

$$S_n = \frac{n}{2} [2a + (n - 1)d]$$

$$T_n = ar^{n-1}$$

$$S_n = \frac{a(r^n - 1)}{r - 1}; r \neq 1$$

$$S_\infty = \frac{a}{1 - r}; -1 < r < 1$$

$$F = \frac{x[(1+i)^n - 1]}{i}$$

$$P = \frac{x[1 - (1+i)^{-n}]}{i}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$M\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$y = mx + c$$

$$y - y_1 = m(x - x_1)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \tan \theta$$

$$(x - a)^2 + (y - b)^2 = r^2$$

$$\text{In } \Delta ABC: \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\text{area } \Delta ABC = \frac{1}{2} ab \sin C$$

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

$$\cos 2\alpha = \begin{cases} \cos^2 \alpha - \sin^2 \alpha \\ 1 - 2\sin^2 \alpha \\ 2\cos^2 \alpha - 1 \end{cases} \quad \sin 2\alpha = 2 \sin \alpha \cos \alpha$$

$$\bar{x} = \frac{\sum fx}{n}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$



$$P(A) = \frac{n(A)}{n(S)}$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$\hat{y} = a + bx$$

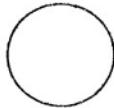
$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$



SC/NSC Answer Book
SS/NSS-antwoordeboek

Senior Certificate/National Senior Certificate/Senior Sertifikaat/Nasionale Senior Sertifikaat (Grade 12/Graad 12) 2023

CENTRE NUMBER SENTRUMNOMMER						
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EXAMINATION NUMBER EKSAMENNOMMER											
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DATE DATUM	
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BOOK NUMBER BOEKNUMMER		OF VAN		BOOKS BOEKЕ
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SUBJECT CODE VAKKODE				
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PAPER NUMBER VRAESTELNOMMER	2
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SUBJECT NAME VAKNAAM	MATHEMATICS/WISKUNDE
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MARKER/NASIEENER			MODERATOR'S INITIALS IN RELEVANT BLOCK MODERATOR SE VOORLETTERS IN RELEVANTE BLOKKIE									
Question Vraag	Marks Punte	Marker's Code & Initials Nasieners se Kode & Voorletters	Marks Punte	SM	Marks Punte	DCM AHN	Marks Punte	CM HIN	Marks Punte	IM	Marks Punte	EM
1												
2												
3												
4												
5												
6												
7												
8												
9												
10												
TOTAL TOTAAL												

CONTROLLED AND CERTIFIED CORRECT (SURNAME AND INITIALS OF EA) GEKONTROLEER EN AS KORREK GESERTIFISEER (VAN EN VOORLETTERS VAN EA)		READ INSTRUCTIONS ON THE NEXT PAGE LEES INSTRUKSIES OP VOLGENDE BLADSYE.
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This answer book consists of 24 pages./Hierdie antwoordeboek bestaan uit 24 bladsye.



PLEASE FOLLOW THESE INSTRUCTIONS CAREFULLY	VOLG ASSEBLIEF HIERDIE INSTRUKSIES NOUKEURIG
<p>1. Clearly write your examination number and centre number in the space provided and attach your barcode label in the space provided.</p>  <p>2. Remember that your own name (or the name of your school) may not appear anywhere on or in this answer book.</p> <p>3. Answer ALL questions in the spaces provided.</p> <p>4. No pages may be torn from this answer book.</p> <p>5. Read the instructions printed on your timetable carefully as well as any other instructions which may be given in each examination paper.</p> <p>6. Candidates may not retain an answer book or remove it from the examination room.</p> <p>7. Answers must be written in black/blue ink as distinctly as possible. Do not write in the margins.</p> <p>8. Write the numbers of the questions you have answered on the front cover of the answer book where marks are to be recorded.</p> <p>9. If you require additional space for your answers:</p> <ul style="list-style-type: none"> 9.1 Use the additional space provided at the end of the answer book. 9.2 When answering a question in the additional space, indicate clearly the question number in the column on the LHS. 9.3 Rule off after each answer. <p>10. Draw a neat line through any work/rough work that must not be marked.</p>	<p>1. Skryf jou eksamen nommer en sentrum nommer duidelik in die ruimtes verskaf en plak jou stafieskodeplakker in die ruimte verskaf.</p> <p>2. Onthou dat jou eie naam (of die naam van jou skool) nie op of in hierdie antwoordeboek mag voorkom nie.</p> <p>3. Beantwoord ALLE vrae in die ruimtes wat voorsien is.</p> <p>4. Geen bladsye mag uit hierdie antwoordeboek geskeur word nie.</p> <p>5. Lees die instruksies wat op jou eksamenrooster gedruk is, sorgvuldig deur, asook enige ander instruksies wat op elke eksamenvraestel gegee word.</p> <p>6. Geen antwoordeboek mag deur die kandidaat behou of uit die eksamenlokaal verwyder word nie.</p> <p>7. Skryf die antwoorde so duidelik moontlik met swart/blou ink. Laat die kantlyne oop.</p> <p>8. Skryf die nommers van die vrae wat jy beantwoord het op die voorblad van die antwoerdeboek waar die punte aangebring word.</p> <p>9. In geval jy bykomende ruimte benodig vir jou antwoorde:</p> <ul style="list-style-type: none"> 9.1 Gebruik die bykomende ruimte wat aan die einde van die antwoerdeboek voorsien word. 9.2 As 'n vraag in die bykomende ruimte beantwoord word, dui duidelik die vraagnommer in die kolom aan die LK aan. 9.3 Trek 'n lyn na elke antwoord. <p>10. Trek 'n netjiese lyn deur enige werk/rofwerk wat nie nagesien moet word nie.</p> 



QUESTION/VRAAG 1

1.1

Amount spent on advertising (in rands)/ <i>Bedrag aan advertensies spandeer (in rand) (x)</i>		21 300	23 700	24 800	30 540	24 100	40 680	22 400	35 250	29 110
Sales (in rands)/ <i>Verkope (in rand) (y)</i>		311 500	326 700	349 200	470 000	316 100	564 200	314 000	487 300	392 900

	<i>Solution/Oplossing</i>	<i>Marks/Punte</i>
1.1.1		
1.1.2		(3)
1.1.3		(2)
1.1.4		(1)
		(1)



1.2

Profit (in rands)/ Wins (in rand)	110 750	107 376	152 338	244 480	144 021	275 994	121 900	207 636	187 700
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	Solution/ <i>Oplossing</i>	Marks <i>Punte</i>
1.2.1		(2)
1.2.2		(1)
1.2.3		(2)
		[12]



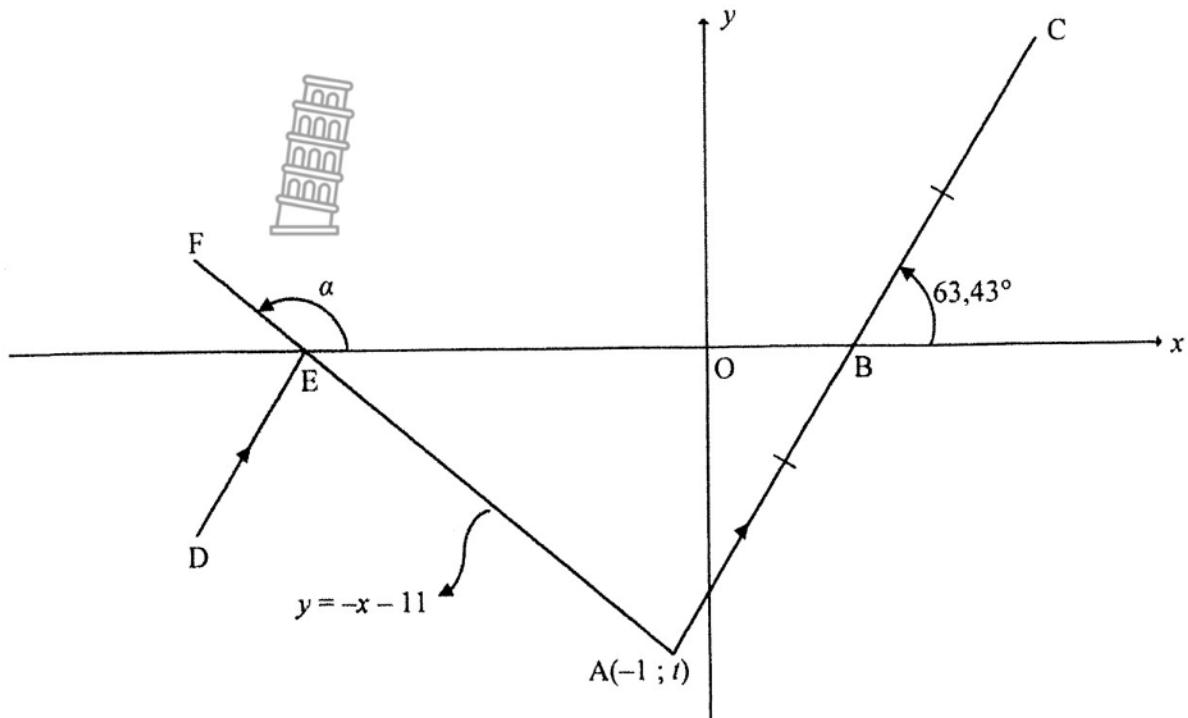
QUESTION/VRAAG 2

AGE/OUDERDOM	NUMBER OF PEOPLE/ GETAL MENSE
$5 < x \leq 15$	20
$15 < x \leq 25$	25
$25 < x \leq 35$	60
$35 < x \leq 45$	90
$45 < x \leq 55$	55
$55 < x \leq 65$	40
$65 < x \leq 75$	30

	Solution/Oplossing	Marks Punte
2.1		
2.2		(1)
2.3	<p style="text-align: center;">OGIVE/OGIEF</p>	(1)
2.4		(4)
		(2) [8]



QUESTION/VRAAG 3



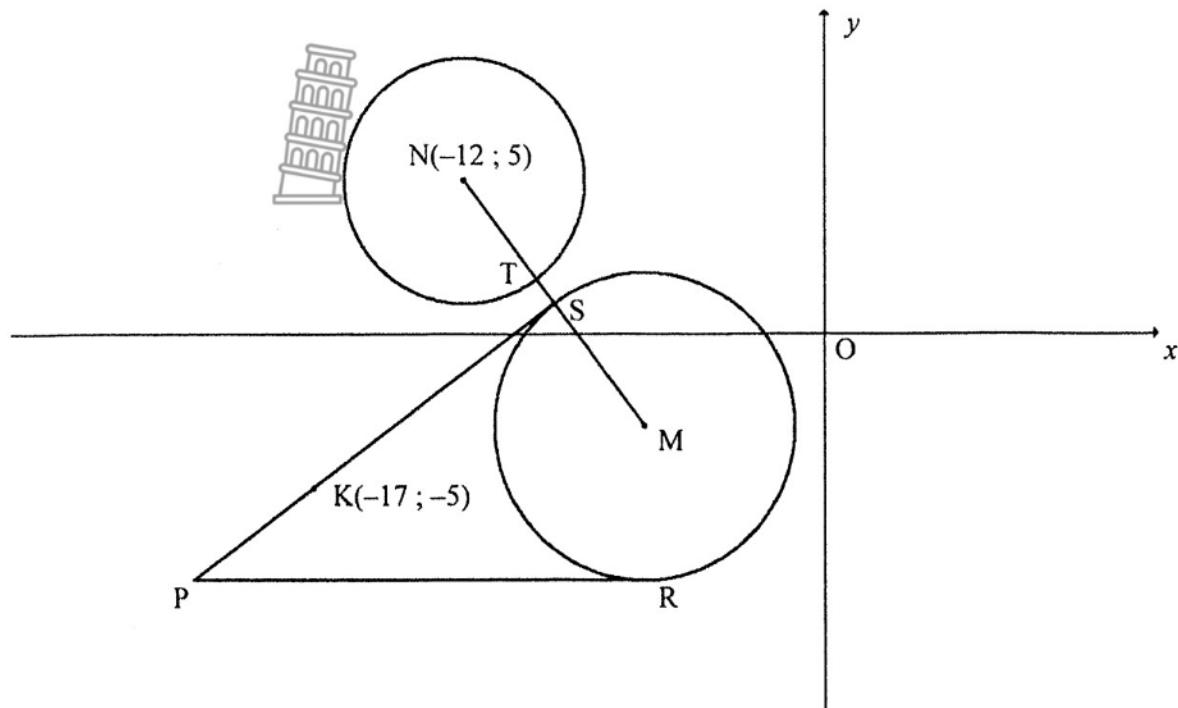
	Solution/Oplossing	Marks/Punte
3.1.1		(2)
3.1.2		(2)
3.1.3		(2)
3.2		(2)



	Solution/Oplossing	Marks/Punte
3.3.1		(3)
3.3.2		(3)
3.4		(4) [18]



QUESTION/VRAAG 4



	Solution/Oplossing	Marks/Punte
4.1		(2)
4.2.1		(2)
4.2.2		(4)



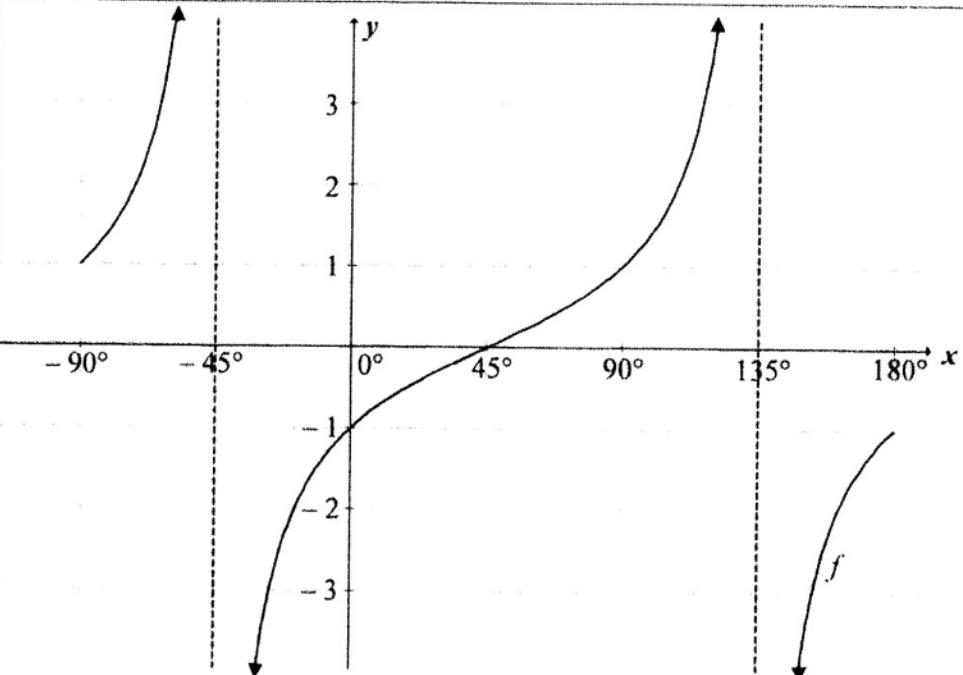
	Solution/ <i>Oplossing</i>	Marks/ Punte
4.3.1		(2)
4.3.2		(5)
4.4.1		
4.4.2		(2) [22]



	Solution/Oplossing	Marks Punte
5.5.1		(4)
5.5.2		(3) [28]



QUESTION/VRAAG 6

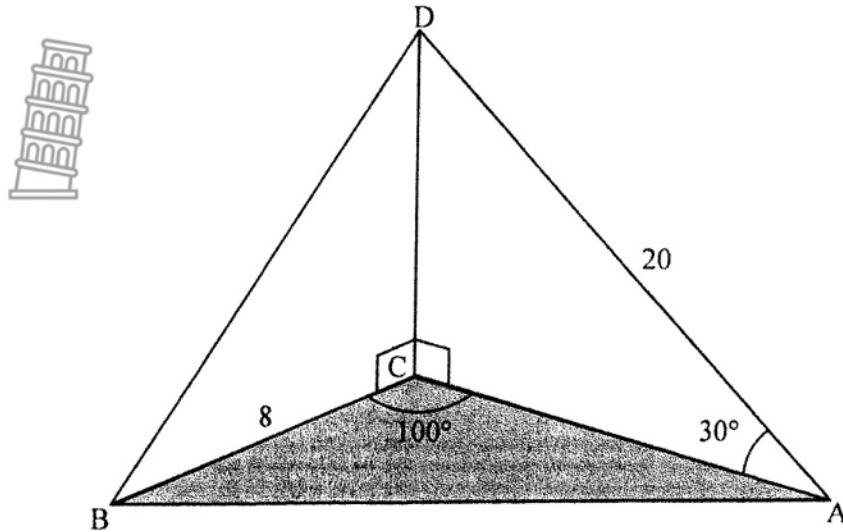
	Solution/Oplossing	Marks/Punte
6.1		
6.2		(1)
6.3		
6.4		(1)
6.5.1		(2)
		(2)



	Solution/Oplossing	Marks/Punte
6.5.2		(4) [13]



QUESTION/VRAAG 7



	Solution/Oplossing	Marks/Punte
7.1.1		
7.1.2		(2)
7.2		(3)
		(3)
		[8]

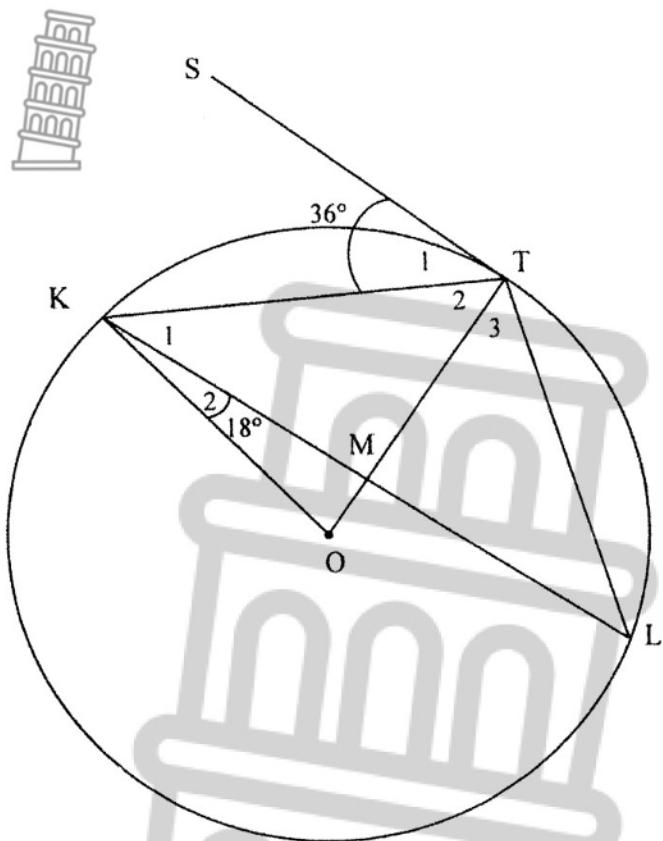


Give reasons for your statements in QUESTIONS 8, 9 and 10.

Gee redes vir jou bewerings in VRAAG 8, 9 en 10.

QUESTION/VRAAG 8

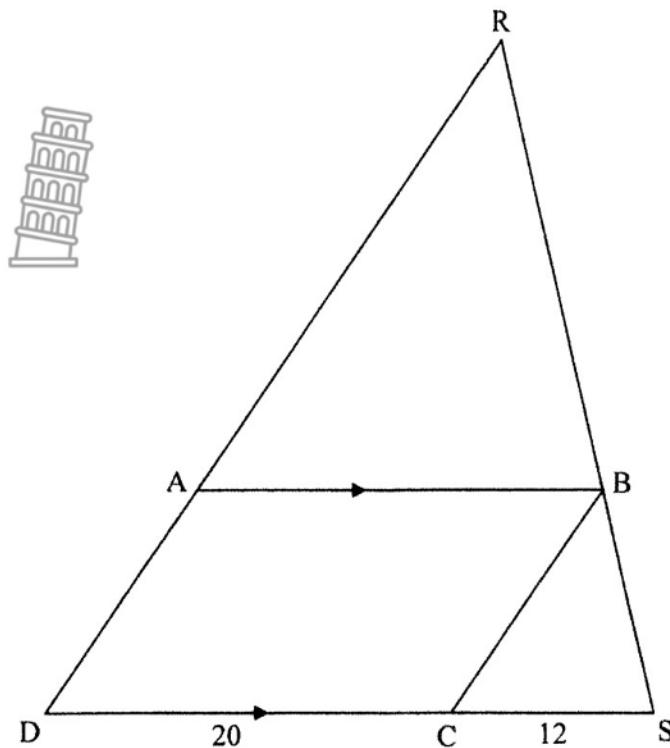
8.1



	Solution/Oplossing	Marks/Punte
8.1.1(a)		(2)
8.1.1(b)		(2)
8.1.1(c)		(2)
8.1.2		(3)



8.2

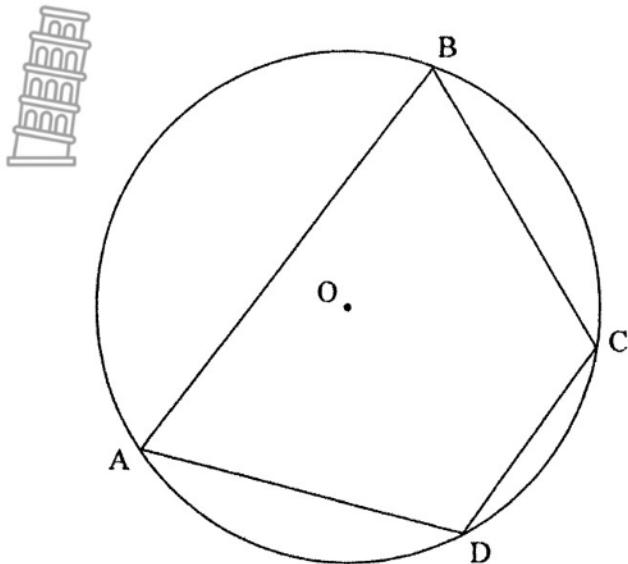


	Solution/Oplossing	Marks Punte
8.2.1		(3)
8.2.2		(3)



QUESTION/VRAAG 9

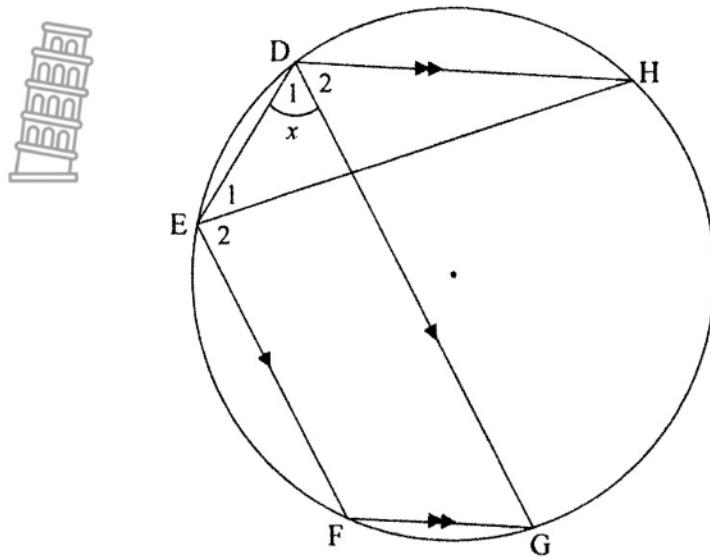
9.1



	Solution/Oplossing	Marks/Punte
		(5)



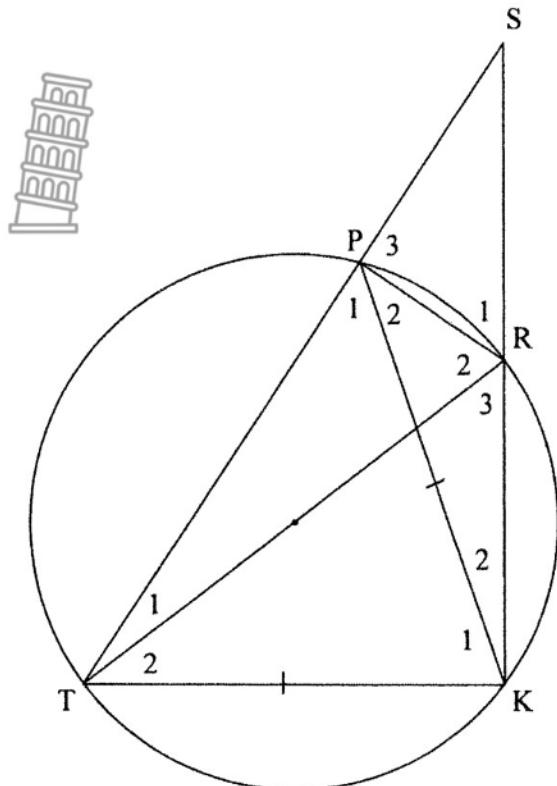
9.2



	Solution/Oplossing	Marks/Punte
		(4) [9]



QUESTION/VRAAG 10



	Solution/ <i>Oplossing</i>	Marks/ <i>Punte</i>
10.1.1		(4)
10.1.2		(5)



	Solution/Oplossing	Marks/Punte
10.1.3		(3)
10.2		(5) [17]







TOTAL/TOTAAL: 150





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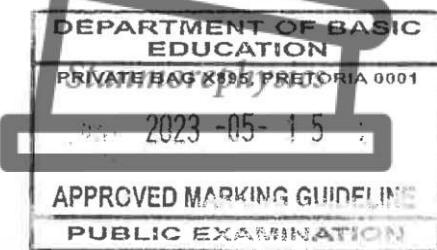
Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

SENIOR CERTIFICATE EXAMINATIONS/ *SENIORSERTIFIKAAT-EKSAMEN* NATIONAL SENIOR CERTIFICATE EXAMINATIONS/ *NASIONALE SENIORSERTIFIKAAT-EKSAMEN*

MATHEMATICS P2/WISKUNDE V2

MARKING GUIDELINES/NASIENRIGLYNE

MAY/JUNE/MEI/JUNIE 2023



MARKS: 150
PUNTE: 150

These marking guidelines consist of 21 pages./
Hierdie nasienriglyne bestaan uit 21 bladsye.

Prof Rajendran Govender

Govender

Approved by Umalusi External Moderator on 15 May 2023

Approved
2023-05-15

G

NOTE:

- If a candidate answers a question TWICE, mark only the FIRST attempt.
- If a candidate has crossed out an attempt at an answer and not redone the question, mark the crossed-out version.
- Consistent accuracy applies in ALL aspects of the marking guidelines. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

LET WEL:

- As 'n kandidaat 'n vraag TWEE KEER beantwoord, sien slegs die EERSTE poging na.
- As 'n kandidaat 'n antwoord van 'n vraag doodtrek en nie oordoen nie, merk die doodgetrekte poging.
- Volgehoue akkuraatheid word in ALLE aspekte van die nasienriglyne toegepas. Hou op nasien by die tweede berekeningsfout.
- Aanvaar van antwoorde/waardes om 'n probleem op te los, word NIE toegelaat nie.

GEOMETRY • MEETKUNDE	
S	A mark for a correct statement <i>(A statement mark is independent of a reason)</i>
R	'n Punt vir 'n korrekte bewering <i>('n Punt vir 'n bewering is onafhanklik van die rede)</i>
S/R	A mark for the correct reason <i>(A reason mark may only be awarded if the statement is correct)</i>
	'n Punt vir 'n korrekte rede <i>('n Punt word slegs vir die rede toegeken as die bewering korrek is)</i>
	Award a mark if statement AND reason are both correct
	<i>Ken 'n punt toe as die bewering EN rede beide korrek is</i>



✓

✓

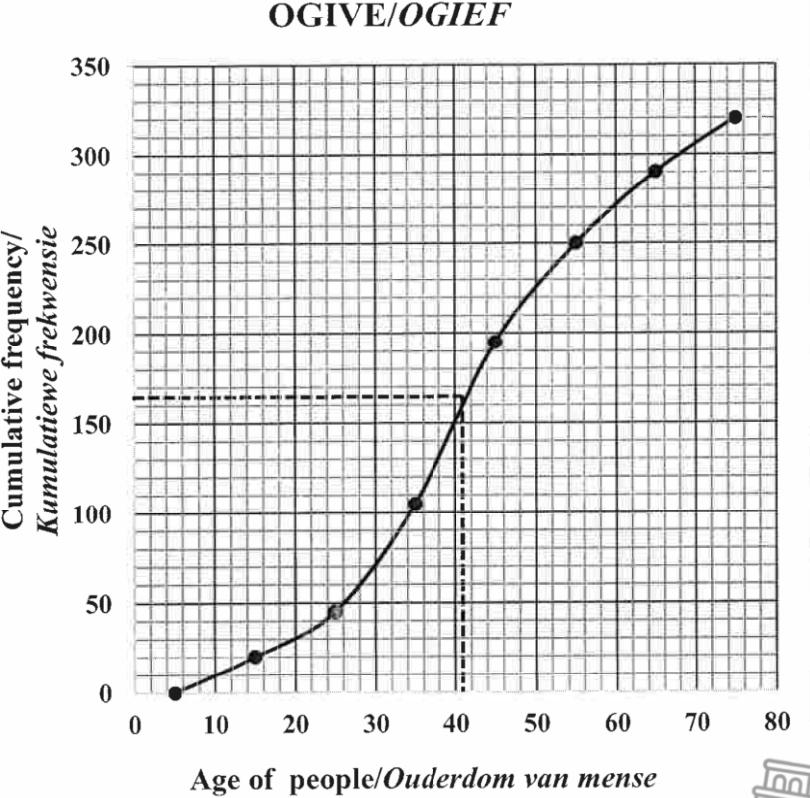
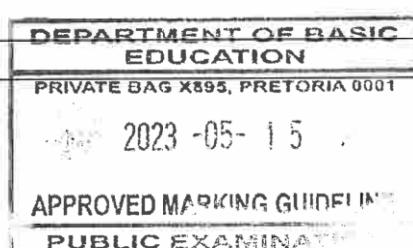
QUESTION/VRAAG 1

1.1.1	$a = 1730,22$ $b = 13,96$ $\hat{y} = 1730,22 + 13,96x$	✓ $a = 1730,22$ ✓ $b = 13,96$ ✓ equation (3)
1.1.2	$\hat{y} = 1730,22 + 13,96x$ $\hat{y} = 1730,22 + 13,96(28500)$ $\hat{y} = R399\ 590,22$ OR/OF $\hat{y} = R399\ 599,64$ (calc)	✓ substitution ✓ answer (2) ✓✓ answer (2)
1.1.3	$r = 0,98002 \dots$ $r = 0,98$	✓ answer (1)
1.1.4	There is a very strong positive correlation between the amount spent on advertising and sales. / <i>Daar is 'n baie sterk positiewe korrelasie tussen die bedrag spandeer op advertensie en die verkope.</i>	✓ strong positive / sterk positief (1)
1.2.1	$\bar{x} = \frac{1552195}{9}$ $\bar{x} = 172466,11$	✓ $\bar{x} = \frac{1552195}{9}$ ✓ answer (2)
1.2.2	$\sigma = 56950,09$	✓ answer (1)
1.2.3	$\bar{x} + \sigma$ $= 172466,11 + 56950,09$ $= 229416,20$ 2 years/jaar	✓ $\bar{x} + \sigma$ ✓ answer (2)
		[12]

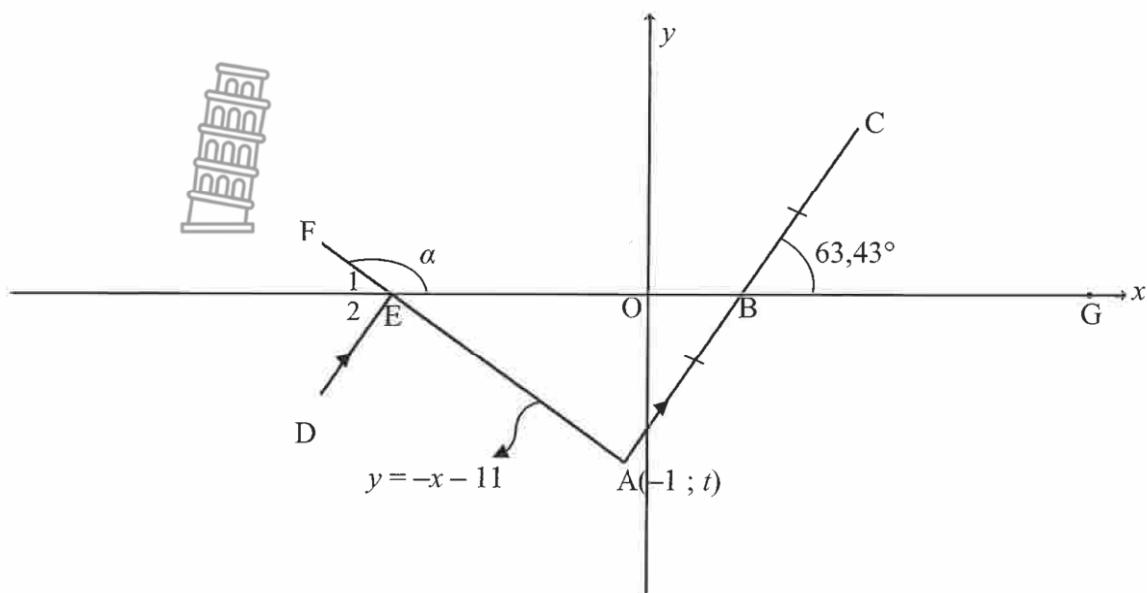


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QUESTION/VRAAG 2

2.1	35 < $x \leq 45$ 	✓ answer (1)																								
2.2	320 people/mense 	✓ answer (1)																								
2.3	<table border="1"> <thead> <tr> <th>AGE</th> <th>NUMBER OF PEOPLE</th> <th>CUMULATIVE FREQUENCY</th> </tr> </thead> <tbody> <tr> <td>5 < $x \leq 15$</td> <td>20</td> <td>20</td> </tr> <tr> <td>15 < $x \leq 25$</td> <td>25</td> <td>45</td> </tr> <tr> <td>25 < $x \leq 35$</td> <td>60</td> <td>105</td> </tr> <tr> <td>35 < $x \leq 45$</td> <td>90</td> <td>195</td> </tr> <tr> <td>45 < $x \leq 55$</td> <td>55</td> <td>250</td> </tr> <tr> <td>55 < $x \leq 65$</td> <td>40</td> <td>290</td> </tr> <tr> <td>65 < $x \leq 75$</td> <td>30</td> <td>320</td> </tr> </tbody> </table>	AGE	NUMBER OF PEOPLE	CUMULATIVE FREQUENCY	5 < $x \leq 15$	20	20	15 < $x \leq 25$	25	45	25 < $x \leq 35$	60	105	35 < $x \leq 45$	90	195	45 < $x \leq 55$	55	250	55 < $x \leq 65$	40	290	65 < $x \leq 75$	30	320	
AGE	NUMBER OF PEOPLE	CUMULATIVE FREQUENCY																								
5 < $x \leq 15$	20	20																								
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65 < $x \leq 75$	30	320																								
	<p style="text-align: center;">OGIVE/OGIEF</p> 	<ul style="list-style-type: none"> ✓ cumulative frequency ✓ grounding ✓ plotting at upper limit ✓ shape (4)																								
2.4	Median = 41	✓✓ answer (2)   [8]																								

QUESTION/VRAAG 3

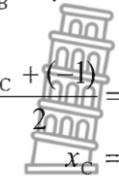


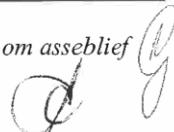
3.1.1	$y = -x - 11$ $A(-1; t)$ $t = -(-1) - 11$ $t = -10$	✓ substitution ✓ value of t (2)
3.1.2	$\tan \alpha = -1$ ref. $\angle = 45^\circ$ $\therefore \alpha = 135^\circ$	✓ $\tan \alpha = -1$ ✓ 135° (2)
3.1.3	$\tan 63,43^\circ = m_{AC}$ $m_{AC} = 2$	✓ $\tan 63,43^\circ = m_{AC}$ ✓ answer (2)
3.2	$m_{AC} = 2$ $A(-1; -10)$ $y = 2x + k$ $-10 = 2(-1) + k$ $k = -8$ $y = 2x - 8$	OR/OF $y - y_1 = 2(x - x_1)$ $y - (-10) = 2(x - (-1))$ $y = 2x - 8$ ✓ substitution of m and A ✓ equation  (2)



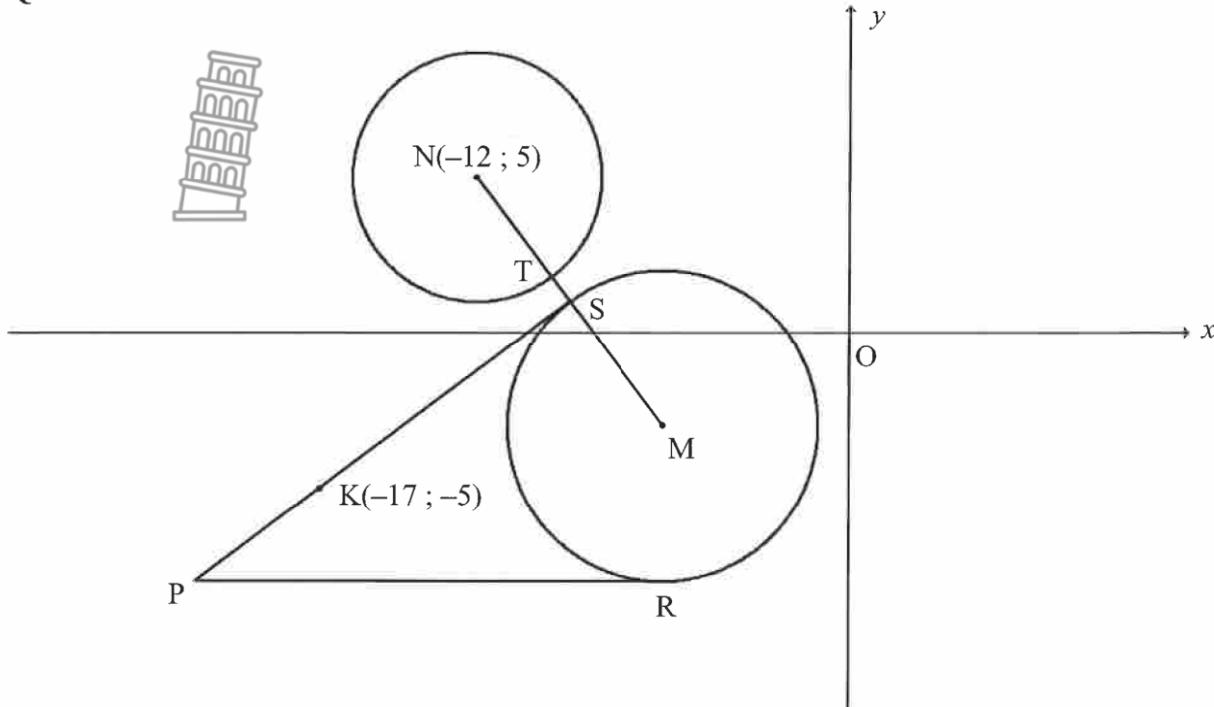
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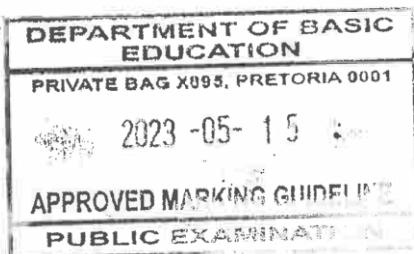
3.3.1	$y = 2x - 8$ $0 = 2x - 8$ $x_B = 4$  $\frac{x_C + (-1)}{2} = 4$ $x_C = 9$ $\frac{y_C + (-10)}{2} = 0$ $y_C = 10$ <p>OR/OF by translation / met translasie</p> $A \rightarrow B (x; y) \rightarrow (x + 5; y + 10)$ $B \rightarrow C (4; 0) \rightarrow (4 + 5; 0 + 10) = (9; 10)$	$\checkmark x_B = 4$ $\checkmark x_C = 9 \quad \checkmark y_C = 10 \quad (3)$ $\checkmark (x+5; y+10)$ $\checkmark x_C = 9 \quad \checkmark y_C = 10 \quad (3)$
3.3.2	$\hat{A}B\hat{E} = 63,43^\circ$ $\hat{E}_2 = 63,43^\circ$ $\hat{E}_1 = 45^\circ$ $\hat{F}\hat{E}D = 108,43^\circ$ <p>OR/OF</p> $\hat{E}\hat{A}B = 135^\circ - 63,43^\circ$ $\hat{E}\hat{A}B = 71,57^\circ$ $\hat{D}\hat{E}A = \hat{E}\hat{A}B = 71,57^\circ$ $\hat{F}\hat{E}D = 108,43^\circ$	$\checkmark \hat{A}B\hat{E} = 63,43^\circ$ $\checkmark \hat{E}_1 = 45^\circ$ $\checkmark \hat{F}\hat{E}D = 108,43^\circ \quad (3)$ $\checkmark \hat{E}\hat{A}B = 71,57^\circ$ $\checkmark \hat{D}\hat{E}A = \hat{E}\hat{A}B = 71,57^\circ$ $\checkmark \hat{F}\hat{E}D = 108,43^\circ \quad (3)$
3.4	$y = 0$ $x_E = -11$ $\frac{x_G + (-11)}{2} = 4$ $x_G = 19$ $(x-19)^2 + y^2 = 15^2$ $(x-19)^2 + y^2 = 225$	$\checkmark x_E = -11$  $\checkmark x_G = 19$ $\checkmark (x-19)^2 + y^2 \checkmark 225 \quad (4)$



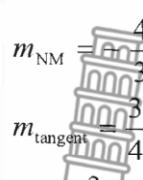
QUESTION/VRAAG 4



4.1	$M(-6; -3)$	✓ -6 ✓ -3 (2)
4.2.1	$x^2 + y^2 + 24x - 10y + 153 = 0$ $(x+12)^2 + (y-5)^2 = -153 + 144 + 25$ $(x+12)^2 + (y-5)^2 = 16$ $r^2 = 16$ $r = 4 \text{ units}$	✓ $r^2 = -153 + 144 + 25$ ✓ length of radius (2)
4.2.2	$NM = \sqrt{(-12 - (-6))^2 + (5 - (-3))^2}$ $NM = 10 \text{ units}$ $SM = 5 \text{ units}$ $\therefore TS = 10 - 5 - 4 = 1 \text{ unit}$	✓ substitution into distance formula ✓ $NM = 10 \text{ units}$ ✓ $SM = 5 \text{ units}$ ✓ answer (4)
4.3.1	$R(-6; -8)$ $y = -8$	✓ $y_R = -8$ ✓ equation (2)



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4.3.2	$m_{NM} = \frac{5 - (-3)}{-12 - (-6)}$  $m_{NM} = \frac{4}{3}$ $m_{\text{tangent}} = \frac{3}{4}$ $-5 = \frac{3}{4}(-17) + c$ OR/OF $y - y_1 = \frac{3}{4}(x - x_1)$ $c = \frac{31}{4}$ $y = \frac{3}{4}x + \frac{31}{4}$	✓ substitution ✓ $m_{NM} = -\frac{4}{3}$ ✓ $m_{\text{tangent}} = \frac{3}{4}$ ✓ substitution of m and N ✓ equation (5)
	OR/OF $NS = SM = 5$ $S\left(\frac{-12-6}{2}; \frac{5-3}{2}\right)$ $S(-9; 1)$ $m_{SK} = \frac{1 - (-5)}{-9 + 17}$ $= \frac{6}{8} = \frac{3}{4}$ $y + 5 = \frac{3}{4}(x + 17)$ $y = \frac{3}{4}x + \frac{31}{4} \text{ or } y = \frac{3}{4}x + 7\frac{3}{4}$	✓ S midpoint ✓ coordinates of S ✓ $m_{\text{tangent}} = \frac{3}{4}$ ✓ substitution of m and $K(-17; -5)$ or S ✓ equation (5)
4.4.1	$-8 = \frac{3}{4}x + \frac{31}{4}$ $-32 = 3x + 31$ $3x = -63$ $x = -21$ $P(-21; -8)$ $R(-6; -8)$ $PR = PS = 15 \text{ units}$ [tangents from same point] $MS = MR = 5 \text{ units}$ $\text{Perimeter PSMR} = 15 + 15 + 5 + 5$ $= 40 \text{ units}$	✓ $-8 = \frac{3}{4}x + \frac{31}{4}$ ✓ $x = -21$ ✓ $PR = PS = 15 \text{ units}$ ✓ $MS = MR = 5 \text{ units}$ ✓ answer (5)

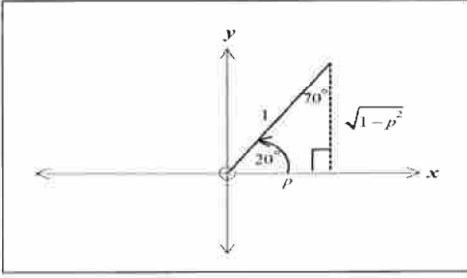


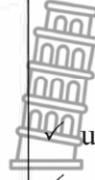
4.4.2 $\frac{\text{area of } \Delta NPS}{\text{area of quadrilateral PSMR}}$ $\frac{\frac{1}{2} NS \cdot SP}{\frac{1}{2} SP \cdot MS + \frac{1}{2} MR \cdot PR}$ $= \frac{\frac{1}{2}(5)(15)}{2\left(\frac{1}{2}\right)(5)(15)}$ $= \frac{1}{2}$ <p>OR</p> $\frac{\Delta NPS \equiv \Delta SPM \equiv \Delta MPR}{\text{area of } \Delta NPS}$ $\frac{\text{area of } \Delta NPS}{\text{area of quadrilateral PSMR}}$ $= \frac{1}{2}$	\checkmark substitution \checkmark answer (2) \checkmark congruent \checkmark answer (2)
	[22]

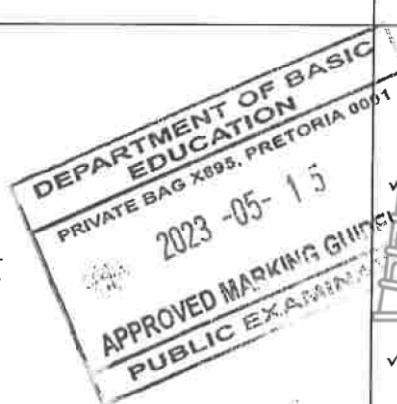
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QUESTION/VRAAG 5

5.1	$ \begin{aligned} & \frac{1 - \sin(\theta)\cos(90^\circ + \theta)}{\cos(\theta - 360^\circ)} \\ &= \frac{1 - (-\sin\theta)(-\sin\theta)}{\cos\theta} \\ &= \frac{1 - \sin^2\theta}{\cos\theta} \\ &= \frac{\cos^2\theta}{\cos\theta} \\ &= \cos\theta \end{aligned} $	$\checkmark -\sin\theta$ $\checkmark \cos\theta$ $\checkmark \cos^2\theta$ \checkmark answer (5)
5.2.1	$ \begin{aligned} & \cos 200^\circ \\ &= -\cos 20^\circ \\ &= -p \end{aligned} $	\checkmark reduction \checkmark answer (2)
5.2.2	$ \begin{aligned} & \sin(-70^\circ) \\ &= -\sin 70^\circ \\ &= -\cos 20^\circ \\ &= -p \end{aligned} $ <p>OR/OF</p> $ \begin{aligned} & \sin(-70^\circ) \\ &= -\sin 70^\circ \\ &= -p \end{aligned} $	\checkmark reduction \checkmark answer (2)
5.2.3	 $ \begin{aligned} & \sin 10^\circ \\ & \cos(2(10^\circ)) = 1 - 2\sin^2 10^\circ \\ & 2\sin^2 10^\circ = 1 - \cos 20^\circ \\ & \sin 10^\circ = \sqrt{\frac{1 - \cos 20^\circ}{2}} \\ & \sin 10^\circ = \sqrt{\frac{1 - p}{2}} \end{aligned} $ <p>OR/OF</p> $ \begin{aligned} & \sin 10^\circ \\ & \sin(30^\circ - 20^\circ) \\ &= \sin 30^\circ \cos 20^\circ - \cos 30^\circ \sin 20^\circ \\ &= \frac{1}{2}p - \frac{\sqrt{3}}{2}\sqrt{1-p^2} = \frac{p - \sqrt{3}\sqrt{1-p^2}}{2} \end{aligned} $	\checkmark double angle \checkmark sin 10° as subject \checkmark answer (3)



	<p>OR/OF</p> $\sin 10^\circ$ $\sin(70^\circ - 60^\circ)$ $= \sin 70^\circ \cos 60^\circ - \cos 70^\circ \sin 60^\circ$ $= p \cdot \frac{1}{2} \sqrt{1-p^2} \times \frac{\sqrt{3}}{2} = \frac{p - \sqrt{3}\sqrt{1-p^2}}{2}$ 	<ul style="list-style-type: none"> ✓ using special angle ✓ expanding ✓ answer (3)
	<p>OR/OF</p> $\sin 10^\circ$ $= \cos 80^\circ$ $\cos(60^\circ + 20^\circ)$ $= \cos 60^\circ \cos 20^\circ - \sin 60^\circ \sin 20^\circ$ $= \frac{1}{2}p - \frac{\sqrt{3}}{2} \cdot \sqrt{1-p^2}$	<ul style="list-style-type: none"> ✓ using special angle ✓ expanding ✓ answer (3)
5.3	$\cos(A+55^\circ)\cos(A+10^\circ) + \sin(A+55^\circ)\sin(A+10^\circ)$ $= \cos[A+55^\circ - (A+10^\circ)]$ $= \cos 45^\circ$ $= \frac{1}{\sqrt{2}} \quad \text{or} \quad \frac{\sqrt{2}}{2}$	<ul style="list-style-type: none"> ✓✓ compound identity ✓ answer (3)
5.4.1	$\text{LHS} = \frac{\cos 2x + \sin 2x - \cos^2 x}{\sin x - 2 \cos x} \qquad \text{RHS} = -\sin x$ $= \frac{\cos^2 x - \sin^2 x + 2 \sin x \cos x - \cos^2 x}{\sin x - 2 \cos x}$ $= \frac{-\sin^2 x + 2 \sin x \cos x}{\sin x - 2 \cos x}$ $= \frac{-\sin x(\sin x - 2 \cos x)}{\sin x - 2 \cos x}$ $= -\sin x$ <p>∴ LHS = RHS</p>	<ul style="list-style-type: none"> ✓ $\cos^2 x - \sin^2 x$ ✓ $2 \sin x \cos x$ ✓ common factor of $-\sin x$ (3)
5.4.2	$\frac{\cos 2x + \sin 2x - \cos^2 x}{-3 \sin^2 x + 6 \sin x \cos x}$ $= \frac{\cos 2x + \sin 2x - \cos^2 x}{-3 \sin x(\sin x - 2 \cos x)}$ $= \frac{\cos 2x + \sin 2x - \cos^2 x}{(\sin x - 2 \cos x)} \times \frac{1}{-3 \sin x}$ $= (-\sin x) \times \frac{1}{-3 \sin x}$ $= \frac{1}{3}$	 <ul style="list-style-type: none"> ✓ common factor of $3 \sin x$ ✓ substitution ✓ answer (3)

5.5.1 $3 \tan 4x = -2 \cos 4x$ $3 \left(\frac{\sin 4x}{\cos 4x} \right) = -2 \cos 4x$ $3 \sin 4x + 2 \cos^2 4x = 0$ $3 \sin 4x + 2(1 - \sin^2 4x) = 0$ $-2 \sin^2 4x + 3 \sin 4x + 2 = 0$ $2 \sin^2 4x - 3 \sin 4x - 2 = 0$ $(2 \sin 4x + 1)(\sin 4x - 2) = 0$ $\sin 4x = -\frac{1}{2} \quad \text{or} \quad \sin 4x \neq 2$	\checkmark identity \checkmark $1 - \sin^2 4x$ \checkmark standard form \checkmark factors (4)
5.5.2 $\sin 4x = -\frac{1}{2}$ <p>ref. $\angle = 30^\circ$</p> $4x = 210^\circ + k \cdot 360^\circ$ $x = 52,5^\circ + k \cdot 90^\circ ; k \in \mathbb{Z}$	$\text{or } 4x = 330^\circ + k \cdot 360^\circ$ $x = 82,5^\circ + k \cdot 90^\circ ; k \in \mathbb{Z}$ $\checkmark 210^\circ ; 330^\circ$ $\checkmark 52,5^\circ ; 82,5^\circ$ $\checkmark k \cdot 90^\circ ; k \in \mathbb{Z}$ (3)
	[28]

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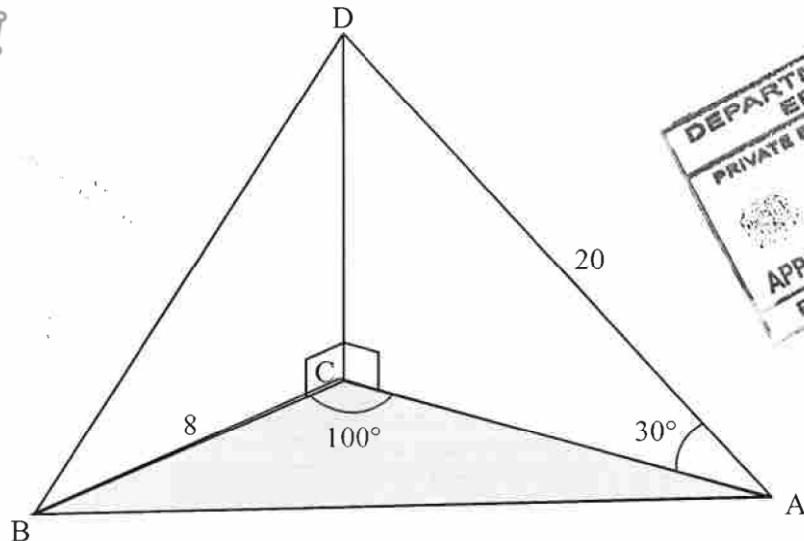
QUESTION/VRAAG 6

6.1	Period = 180°	✓ answer (1)
6.2		✓ x -intercepts ✓ turning points ✓ end points
6.3	$y \in [-1; 1]$ OR/OF $-1 \leq y \leq 1$	✓ answer (1)
6.4	$g(x) = -\cos 2x$ $g(x + 45^\circ) = -\cos 2(x + 45^\circ)$ $= -\cos(2x + 90^\circ)$ $= \sin 2x$	✓ $-\cos 2(x + 45^\circ)$ ✓ answer (2)
6.5.1	$x \in (-90^\circ; -45^\circ)$ OR/OF $-90^\circ < x < -45^\circ$	✓✓ $x \in (-90^\circ; -45^\circ)$ (2)
6.5.2	$2\cos 2x - 1 > 0$ $\cos 2x > \frac{1}{2}$ $-\cos 2x < -\frac{1}{2}$ $x \in (-30^\circ; 30^\circ)$ OR/OF $-30^\circ < x < 30^\circ$	✓ $\cos 2x > \frac{1}{2}$ ✓ $-\cos 2x < -\frac{1}{2}$ ✓ $x = \pm 30^\circ$ ✓ interval (4)
		[13]



Gd

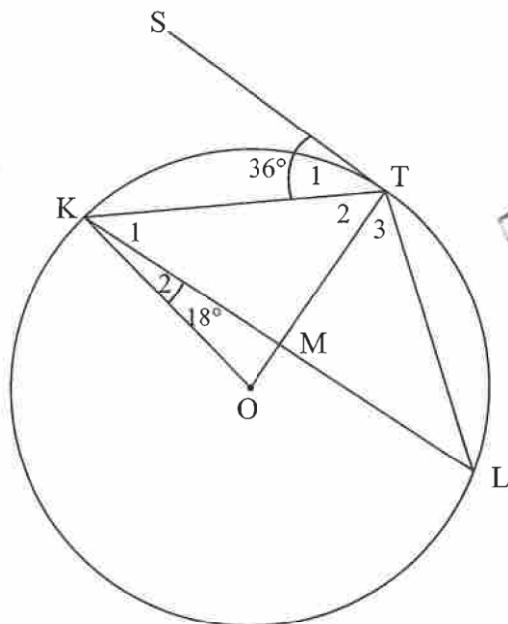
QUESTION/VRAAG 7



7.1.1	$\frac{AC}{20} = \cos 30^\circ$ $AC = 20 \cos 30^\circ$ $AC = 10\sqrt{3} = 17,32 \text{ units}$ <p>OR/OF</p> $\frac{AC}{\sin 60^\circ} = \frac{20}{\sin 90^\circ}$ $\therefore AC = 20 \sin 60 = 17,32$	✓ trig ratio ✓ answer (2)
7.1.2	$AB^2 = AC^2 + BC^2 - 2AC \cdot BC \cos A\hat{C}B$ $AB^2 = (10\sqrt{3})^2 + 8^2 - 2(10\sqrt{3})(8) \cos 100^\circ$ $AB = 20,30 \text{ units}$	✓ cosine formula ✓ substitution into cosine formula ✓ answer (3)
7.2	$\frac{\sin A\hat{D}B}{AB} = \frac{\sin A\hat{B}D}{AD}$ $\frac{\sin A\hat{D}B}{20,3} = \frac{\sin 73,4^\circ}{20}$ $\sin A\hat{D}B = \frac{20,3 \sin 73,4^\circ}{20}$ $A\hat{D}B = 76,58^\circ$	✓ sine formula in ΔABD  ✓ substitution into sine formula ✓ answer (3)
		[8]

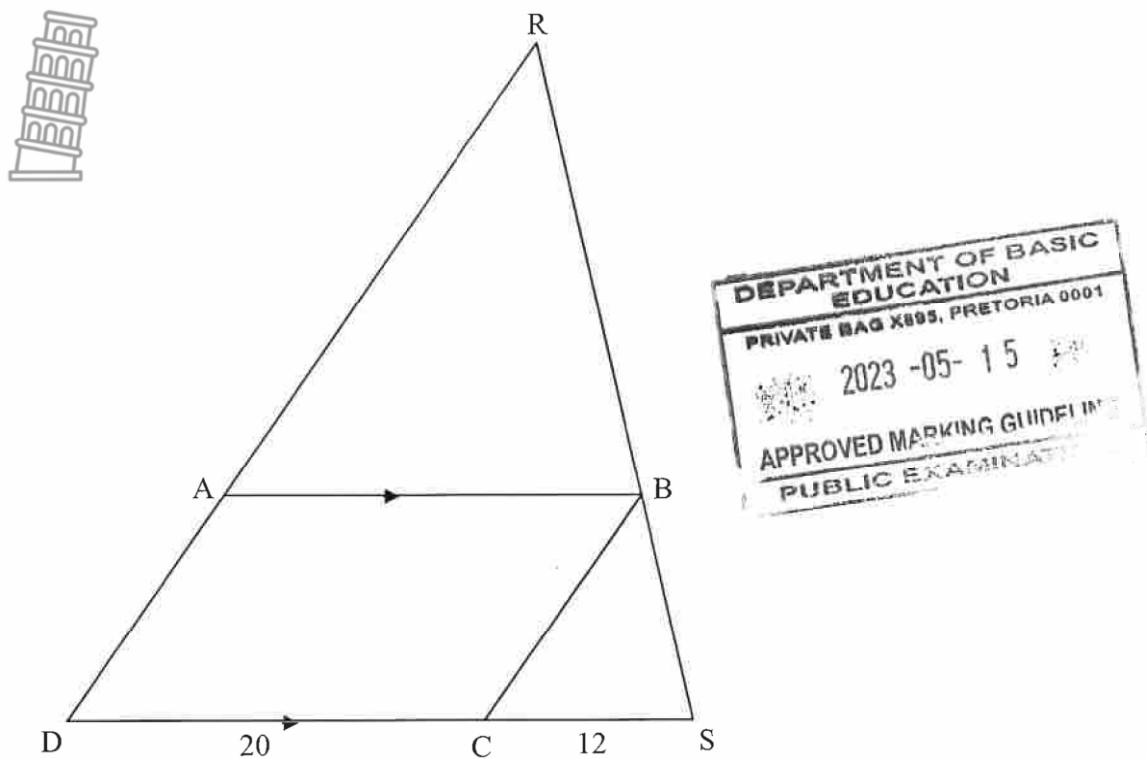
QUESTION/VRAAG 8

8.1



8.1.1(a)	$\hat{T}_2 = 54^\circ$ [tan \perp rad]	✓ S ✓R (2)
8.1.1(b)	$\hat{L} = 36^\circ$ [tan - chord theorem]	✓ S ✓R (2)
8.1.1(c)	$\hat{KOT} = 72^\circ$ [\angle at centre = $2 \times \angle$ at circumference] OR/OF $\hat{OKT} = \hat{T}_2 = 54^\circ$ [\angle s opposite = radii] $\hat{KOT} = 180^\circ - (54^\circ + 54^\circ)$ [sum of int \angle 's of Δ] $= 72^\circ$	✓ S ✓R (2) ✓ S/R ✓ S (2)
8.1.2	$\hat{KMO} = 180^\circ - (18^\circ + 72^\circ)$ $= 90^\circ$ [sum of int \angle 's of Δ] $\therefore KM = ML$ [line from centre \perp to chord]	✓ S ✓ S ✓ R (3)
	 OR/OF $\hat{OKT} = 54^\circ$ [\angle s opposite = radii] $\hat{K}_1 = 54^\circ - 18^\circ = 36^\circ$ $\hat{TMK} = 90^\circ$ [sum of int \angle 's of Δ] $\therefore KM = ML$ [line from centre \perp to chord]	 ✓ S ✓ S ✓ R (3)

8.2



8.2.1	$\frac{DC}{CS} = \frac{20}{12} = \frac{5}{3}$ $\therefore \frac{DC}{CS} = \frac{RB}{BS}$ $\therefore BC \parallel DR \quad [\text{converse line } \parallel \text{ one side of } \Delta \text{ OR sides in the same proportion}]$ $\therefore BC \parallel AD$	✓ S ✓ S ✓ R (3)
8.2.2	$\frac{AR}{AD} = \frac{RB}{BS} \quad [\text{line } \parallel \text{ one side of } \Delta] \text{ OR } [\text{Prop Theorem } AB \parallel DS]$ $\frac{AR}{AD} = \frac{5}{3}$ $\frac{48 - AD}{AD} = \frac{5}{3}$ $\therefore 5AD = 144 - 3AD$ $AD = 18$ $AB = 20 \quad [\text{opp sides of parm}]$ $\therefore AD : AB = 18 : 20 = 9 : 10$	✓ $\frac{AR}{AD} = \frac{5}{3}$ ✓ AD = 18 ✓ ratio (3)

	<p>OR/OF</p> <p></p> $\frac{AR}{RD} = \frac{5}{8}$ <p>.....prop thm AB DS</p> $\frac{AR}{RD} = \frac{5}{8}$ $\frac{48}{48} = \frac{5}{8}$ <p>$\therefore AR = 30$ and $AD = 18$</p> $\therefore \frac{AR}{RD} = \frac{AB}{DS} \dots\dots \parallel \Delta's$ <p>$\therefore AB = 20$</p> $\therefore AB : AD = 18 : 20 = 9 : 10$	
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✓ $\frac{AR}{RD} = \frac{5}{8}$
✓ $AD = 18$

✓ ratio

(3)

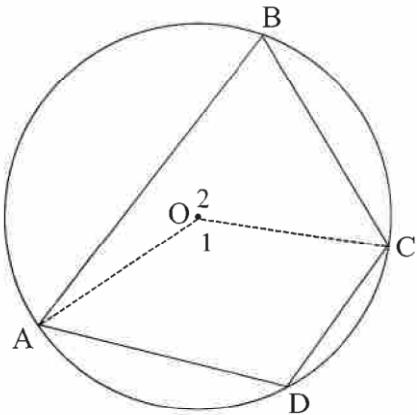
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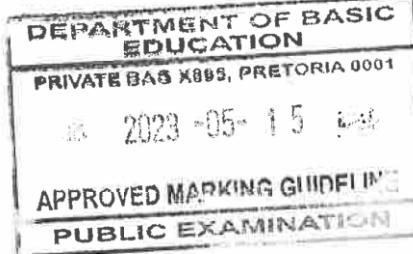


QUESTION/VRAAG 9

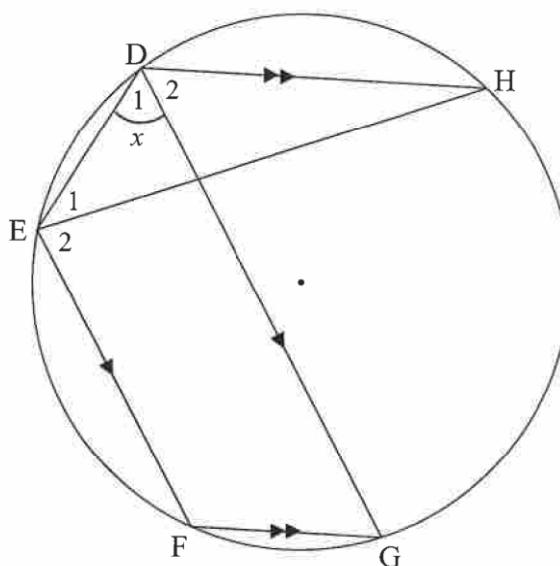
9.1



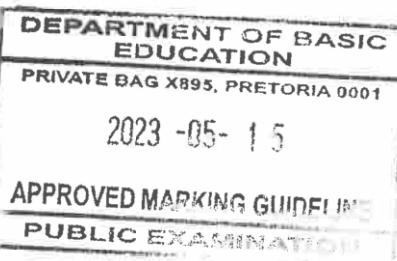
<p>9.1</p> <p>Constr: Draw radii OA and OC.</p> <p>Proof:</p> $\hat{O}_1 = 2\hat{B} \quad [\angle \text{ at centre} = 2 \times \angle \text{ at circumference}]$ $\hat{O}_2 = 2\hat{D} \quad [\angle \text{ at centre} = 2 \times \angle \text{ at circumference}]$ $\hat{O}_1 + \hat{O}_2 = 360^\circ \quad [\text{revolution}]$ $2\hat{B} + 2\hat{D} = 360^\circ \quad [\text{revolution}]$ $\therefore \hat{B} + \hat{D} = 180^\circ$	<p>✓ Construction</p> <p>✓ S ✓ R</p> <p>✓ S/R</p> <p>✓ S</p> <p>(5)</p>
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9.2



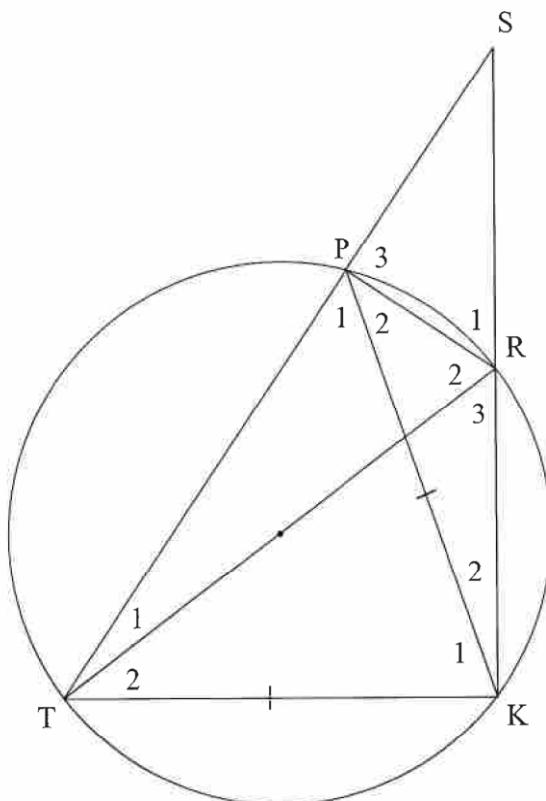
9.2	$E\hat{F}G = 180^\circ - \hat{D}_1$ [opp \angle 's of cyclic quad] $\therefore E\hat{F}G = 180^\circ - x$ $E\hat{F}G = 180^\circ - \hat{G}$ [co-int \angle 's; $EF \parallel DG$] $\hat{G} = x$ But $\hat{G} = \hat{D}_2$ [alt \angle 's; $DH \parallel FG$] $\therefore \hat{D}_1 = \hat{D}_2 = x$	$\checkmark S \checkmark R$ $\checkmark S / R$ $\checkmark S / R$	(4)
			[9]



Gd

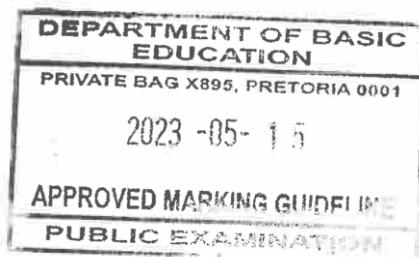
QUESTION/VRAAG 10

10.1



10.1.1	$\hat{TPR} = 90^\circ$ $\hat{SPR} = 90^\circ$ $\therefore SR$ is a diameter	[\angle in semi-circle] [\angle 's on a straight line] [converse \angle in semi-circle]	✓S ✓R ✓S ✓R
	OR $\hat{TKR} = 90^\circ$ $\hat{SPR} = 90^\circ$ $\therefore SR$ is a diameter	[\angle in semi-circle] [ext \angle of cyclic quad] [converse \angle in semi-circle] – OR [chord subtends a right angle]	✓S ✓R ✓S ✓R

10.1.2	$\hat{R}_1 = P\hat{T}K$ $\hat{P}_1 = P\hat{T}K = \hat{R}_1$ $\hat{S} + \hat{R}_1 = \hat{P}_1 + P_2$ $\therefore \hat{S} = \hat{P}_2$	[ext \angle of cyclic quad] [\angle s opp equal sides] [ext \angle of Δ] [$\hat{R}_1 = \hat{P}_1$]	✓S ✓R ✓S /R ✓S ✓R (5)
10.1.3	In ΔSPK and ΔPRK  $\hat{S} = \hat{P}_2$ $\hat{K}_2 = \hat{K}_2$ $\Delta SPK \parallel\!\!\! \Delta PRK$ OR/OF In ΔSPK and ΔPRK $\hat{S} = \hat{P}_2$ $\hat{K}_2 = \hat{K}_2$ $\hat{S}\hat{P}\hat{K} = \hat{P}\hat{R}\hat{K}$ $\Delta SPK \parallel\!\!\! \Delta PRK$	[proved] [common] [\angle, \angle, \angle] ✓S/R (3)	✓S ✓S ✓S/R (3)
10.2	$\frac{PK}{RK} = \frac{SK}{PK}$ [$\Delta SPK \parallel\!\!\! \Delta PRK$] $PK^2 = SK \cdot RK$ $ST^2 = SK^2 + TK^2$ [Pythagoras] $TK = PK$ [Given] $ST^2 = SK^2 + PK^2$ $ST^2 = SK^2 + SK \cdot RK$ $ST^2 = (2RK)^2 + 2RK \cdot RK$ $ST^2 = 6RK^2$ $ST = \sqrt{6}RK$	✓S ✓S ✓PK ² = SK.RK ✓SK = 2RK ✓ST ² = 6RK ² (5)	✓S ✓S ✓PK ² = SK.RK ✓SK = 2RK ✓ST ² = 6RK ² (5)
			[17]



TOTAL/TOTAAL: 150



Go

