



education

Department of
Education
FREE STATE PROVINCE

GRADE 12

MATHEMATICS

GRADE 12

MOCK EXAM

PAPER 2

18 AUGUST 2023

Stanmorephysics

MARKS: 150

DURATION: 3 HOURS

This question paper consists of 15 pages.

INSTRUCTIONS AND INFORMATION

Read the following instructions carefully before answering the questions.

1. This question paper consists of 9 questions.
2. Answer ALL the questions.
3. Number the answers correctly according to the numbering system used in this question paper.
4. Clearly show ALL calculations, diagrams, graphs, etc. which you have used in determining your answers.
5. Answers only will NOT necessarily be awarded full marks.
6. You may use an approved scientific calculator (non-programmable and non-graphical), unless otherwise stated.
7. If necessary, round off answers to TWO decimal places, unless stated otherwise



QUESTION 1

The speeds, in kilometres per hour, of cyclists that passed a point on the route of the Ironman Race were recorded and summarised in the table below:

Speed (km/h)	Frequency (<i>f</i>)	Cumulative Frequency
$0 < x \leq 10$	10	10
$10 < x \leq 20$		30
$20 < x \leq 30$	45	
$30 < x \leq 40$	72	
$40 < x \leq 50$		170

- 1.1 Complete the above table in the ANSWER BOOK provided. (2)
- 1.2 Make use of the axes provided in the ANSWER BOOK to draw a cumulative frequency curve for the above data. (3)
- 1.3 Indicate clearly on your graph where the estimates of the lower quartile (Q_1) and median (M) speeds can be read off. Write down these estimates. (2)
- 1.4 Draw a box and whisker diagram for the data. Use the number line in the ANSWER BOOK. (2)
- 1.5 Use your graph to estimate the number of cyclists that passed the point with speeds greater than 35 km/h. (1)

[10]

QUESTION 2

During the month of June patients visited a number of medical facilities for treatment.

The table shows the number of patients treated on certain dates during the month of June

Dates in the month of June	3	5	8	12	15	19	22	26
Number of patients treated	270	275	376	420	602	684	800	820

- 2.1 On **DIAGRAM SHEET 2**, draw a scatter plot of the given data. (3)
- 2.2 Determine the equation of the least squares regression line of patients treated (y) against date (x). (3)
- 2.3 Estimate how many patients have been treated on the 24th of June. (2)
- 2.4 Draw the least squares regression line on the grid on **DIAGRAM SHEET 2**. (3)

2.5 Calculate the correlation coefficient of the data. Comment on the strength of the relationship between the variables. (3)

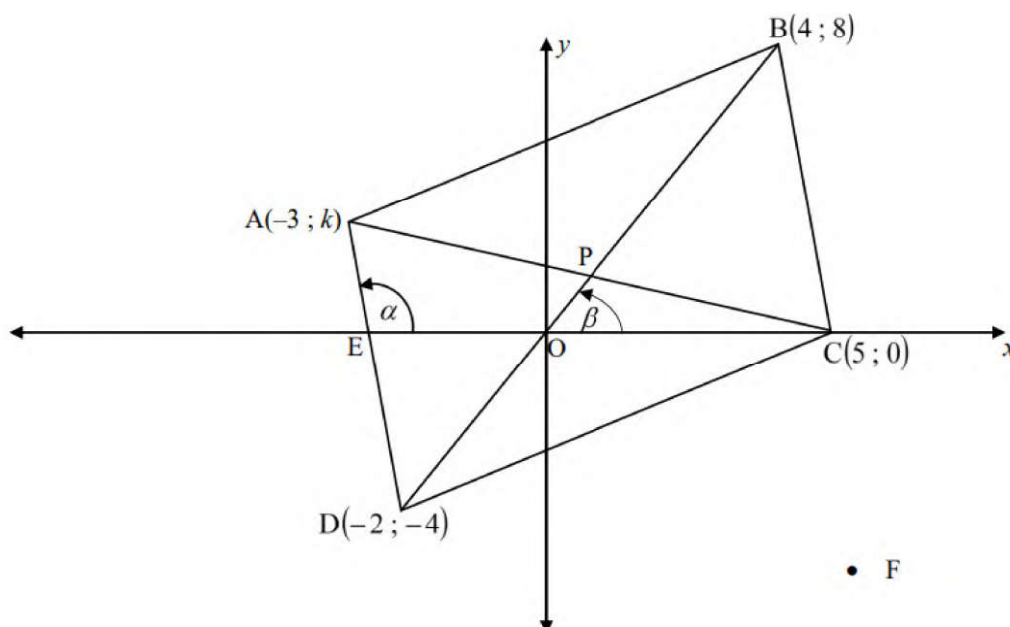
2.6 Given that the mean for patients treated on certain dates is 528,63 calculate how many patients were within one deviation of the mean (3)



[17]

QUESTION 3

In the diagram below, $A(-3; k)$, $B(4; 8)$, $C(5; 0)$ and $D(-2; -4)$ are vertices of the parallelogram $ABCD$. Diagonals AC and BD bisect each other at P . The angles of inclination of AD and BD are α and β respectively. AD cuts the x -axis at E . F is a point in the fourth quadrant.



3.1 Determine the gradient of BC . (2)

3.2 If the distance between points $A(-3; k)$ and $B(4; 8)$ is 65, calculate the value of k . (4)

3.3 Prove, using analytical geometry methods, that $BP \perp AC$. (3)

3.4 Calculate the coordinates of F if it is given that $ACFD$ is a parallelogram. (2)

3.5 Calculate the size of \hat{EDO} (correct to ONE decimal place). (6)

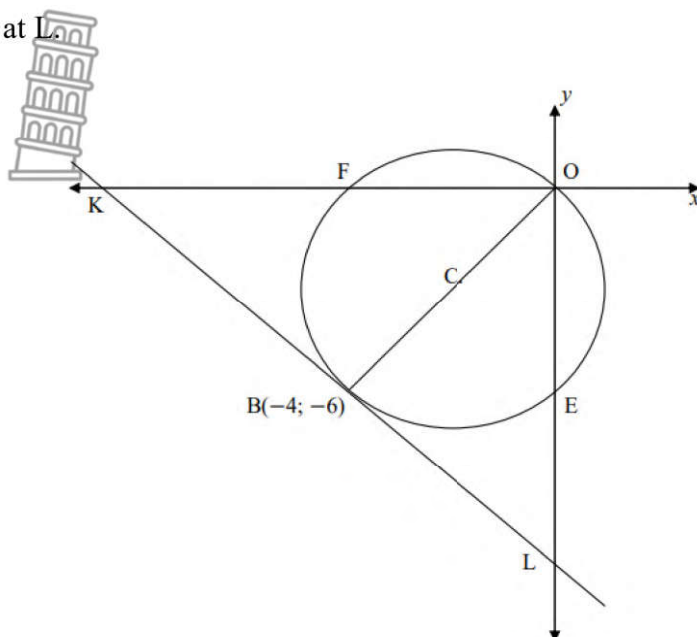
3.6 Calculate the area of $\triangle ADC$. (4)



[21]

QUESTION 4

4. A circle with centre at C passes through the origin, O, and also intersects the x-axis at F and the y-axis at E. The tangent to the circle at B (4 ; 6) intersects the x-axis at K and the y-axis at L.



- 4.1 Calculate the length of the radius of the circle. (3)
- 4.2 Determine the equation of the circle in the form $(x - a)^2 + (y - b)^2 = r^2$. (4)
- 4.3 What type of a triangle is $\triangle OBL$? Give reason for your answer. (2)
- 4.4 Determine the equation of the tangent KL. (4)
- 4.5 Determine the co-ordinates of E. (2)
- 4.2.6 Determine whether EF is a diameter of the circle. Show all working. (5)

[20]

QUESTION 5

- 5.1 If $\tan 58^\circ = m$, determine the following in terms of m without using a calculator.

5.1.1 $\sin 58^\circ$ (2)

5.1.2 $\sin 296^\circ$ (3)

5.1.3 $\cos 2^\circ$ (3)



- 5.2 If $5 \tan \theta + 2\sqrt{6} = 0$ and $0^\circ < \theta < 270^\circ$, determine with the aid of a sketch and without using the calculator, the value of:

5.2.1 $\sin \theta$ (2)

5.2.2 $\cos \theta$ (1)

5.1.3 $\frac{14 \cos \theta + 7\sqrt{6} \sin \theta}{\cos(-240^\circ) \tan 225^\circ}$ (4)



[15]

QUESTION 6

5.1 Determine the value of $\frac{\cos(180^\circ + x) \cdot \tan(360^\circ - x) \cdot \sin^2(90^\circ - x)}{\sin(180^\circ - x)} + \sin^2 x$ (6)

5.2.1 Prove the identity: $\cos(A - B) - \cos(A + B) = 2 \sin A \sin B$ (3)

5.2.2 Hence calculate, without using a calculator, the value of $\cos 15^\circ - \cos 75^\circ$ (4)

5.3 Find the value of $\tan \theta$, if the distance between $A(\cos \theta; \sin \theta)$ and $B(6; 7)$ is $\sqrt{86}$. (4)

[17]

QUESTION 7

Consider: $f(x) = \cos(x - 45^\circ)$ and $f(x) = \tan \frac{1}{2}x$ for $x \in [-180^\circ; 180^\circ]$

6.1 Use the grid provided to draw sketch graphs of f and g on the same set of axes for $x \in [-180^\circ; 180^\circ]$. Show clearly all the intercepts on the axes, the coordinates of the turning points and the asymptotes. (6)

6.2 Use your graphs to answer the following questions for $x \in [-180^\circ; 180^\circ]$

6.2.1 Write the solutions of $\cos(x - 45^\circ) = 0$ (2)

6.2.2 Write down the equations of asymptote(s) of g . (2)

6.2.3 Write down the range of f . (1)

6.2.4 How many solutions exist for the equation $\cos(x - 45^\circ) = \tan \frac{1}{2}x$? (1)

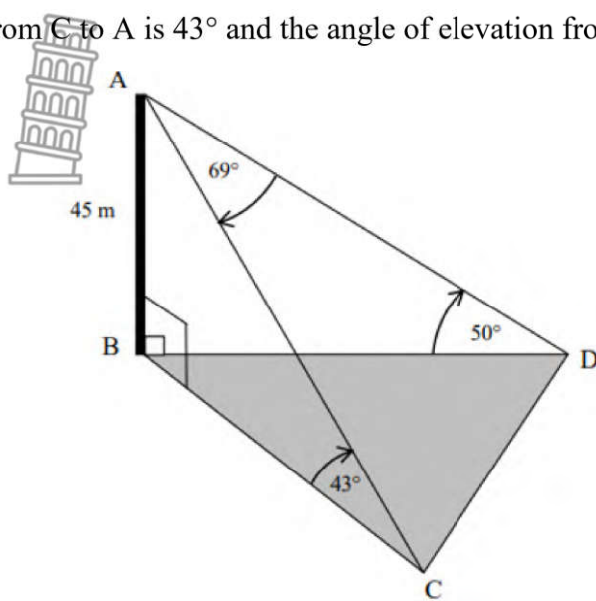
6.2.5 For what value(s) of x is $f(x) \cdot g(x) > 0$? (3)



[15]

QUESTION 7

In the figure below Thabo is standing at a point A on top of building AB that is 45 m high. He observes two cars at C and D respectively. The cars at C and D are in the same horizontal plane as B. The angle of elevation from C to A is 43° and the angle of elevation from D to A is 50° and $\angle CAD = 69^\circ$



- 7.1 Calculate the lengths of AC and AD, correct to 2 decimal places. (4)
- 7.2 Calculate the distance between the two cars, the length of CD. (3)
- [7]

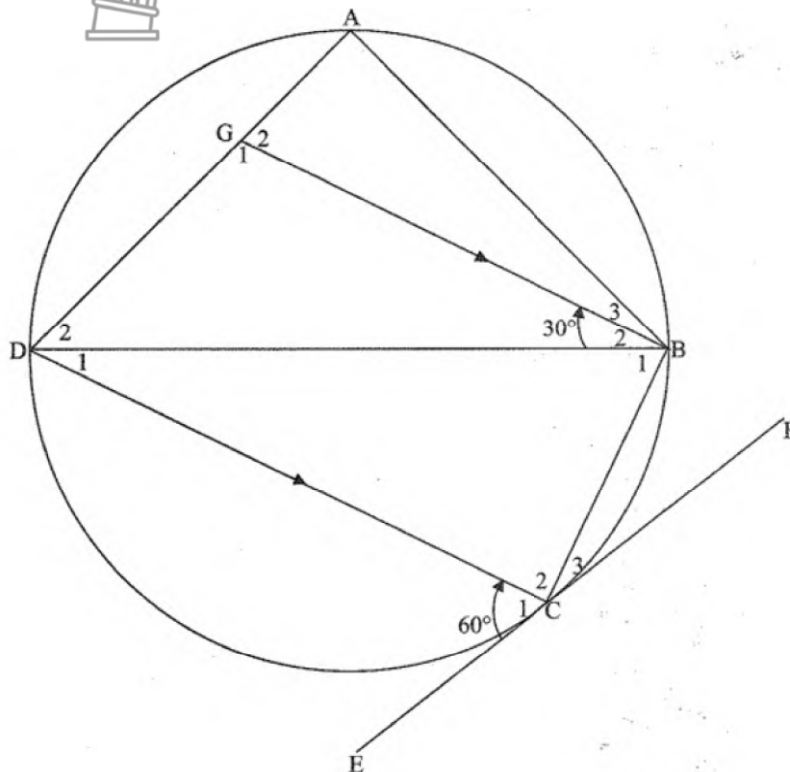


QUESTION 8

PROVIDE REASONS FOR ALL YOUR STATEMENTS AND CALCULATIONS IN QUESTION 8, 9 AND 10

In the diagram, ABCD is a cyclic quadrilateral. G is a point on AD such that $BG \parallel CD$. ECF

is a tangent to the circle at C. BD is a chord of the circle. $\angle GBD = 30^\circ$ and $\angle DCE = 60^\circ$



8.1 Calculate, with reasons, the size of:

8.1.1 $\angle D_1$ (1)

8.1.2 $\angle B_1$ (2)

8.1.3 $\angle C_2$ (1)

8.1.4 $\angle DAB$ (2)

8.2 Is BD a diameter of the circle? Motivate your answer.

(2)

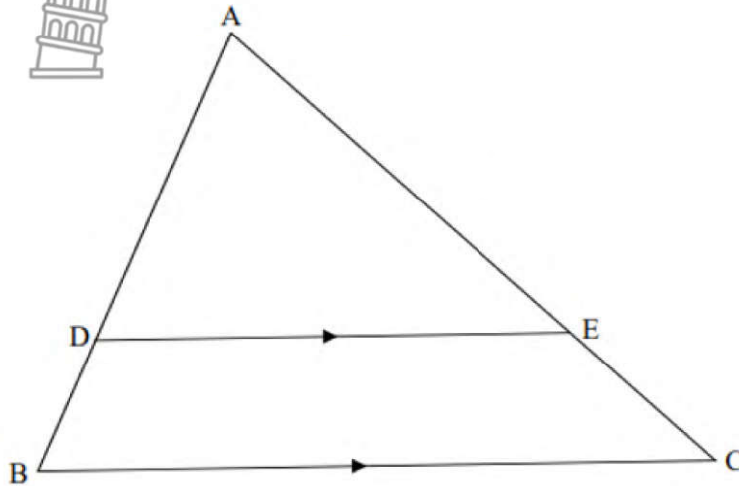
[8]



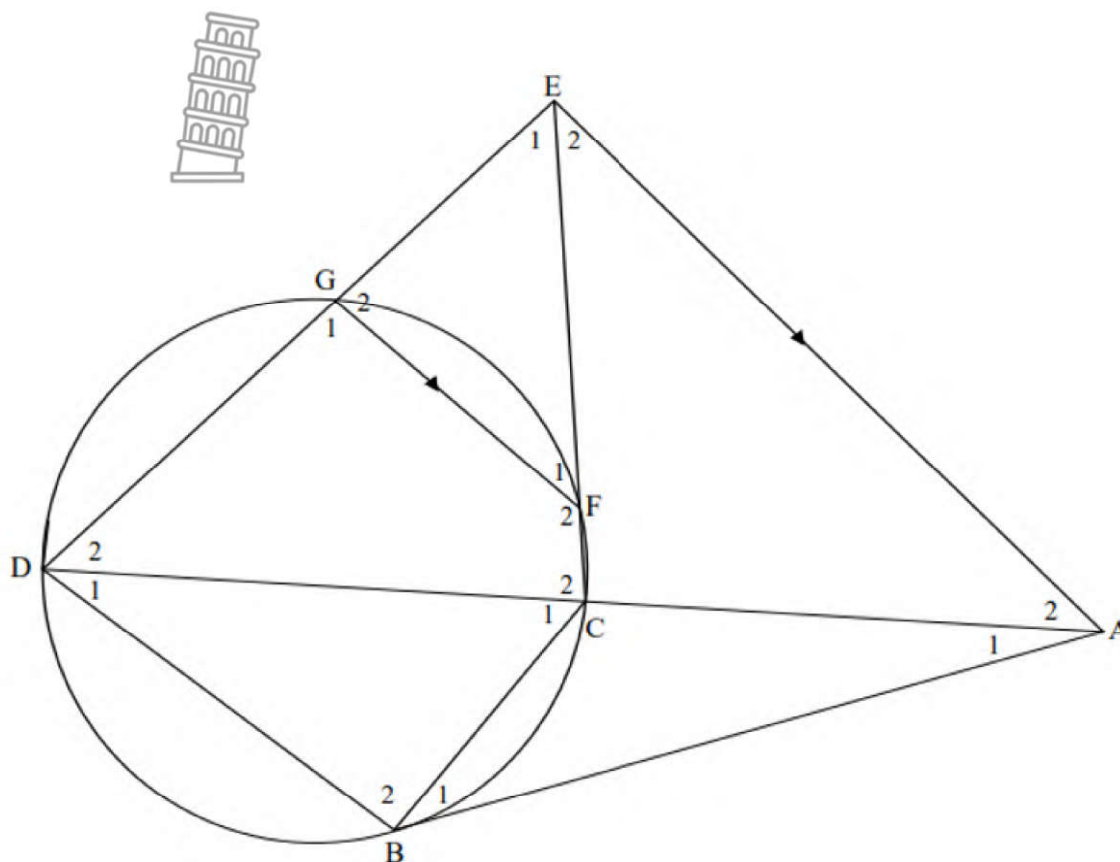
QUESTION 9

9.1 In $\triangle ABC$ below, D and E are points on AB and AC respectively such that

DE \parallel BC. Prove the theorem that states that $\frac{AD}{DB} = \frac{AE}{EC}$ (6)



- 9.2 In the diagram below, DGFC is a cyclic quadrilateral and AB is a tangent to the circle at B. 2
Chords BD and BC are drawn. DG and CF produced meet at E and DC is produced to A.
EA || GF.



- 9.2.1 Give a reason why $\hat{B}_1 = \hat{D}_1$ (1)
- 9.2.2 Prove that $\triangle ABC \parallel \triangle ADB$. (3)
- 9.2.3 Prove $\hat{E}_2 = \hat{D}_2$ (4)
- 9.2.4 Prove $AE^2 = AD \times AC$ (4)
- 9.2.5 Hence, deduce that $AE = AB$ (3)

[21]



SCHOOL NAME: _____

Name : _____ Grade 12 _____



Speed (km/h)	Frequency (f)	Cumulative Frequency
$0 < x \leq 10$	10	10
$10 < x \leq 20$		30
$20 < x \leq 30$	45	
$30 < x \leq 40$	72	
$40 < x \leq 50$		170



QUESTION 1.2

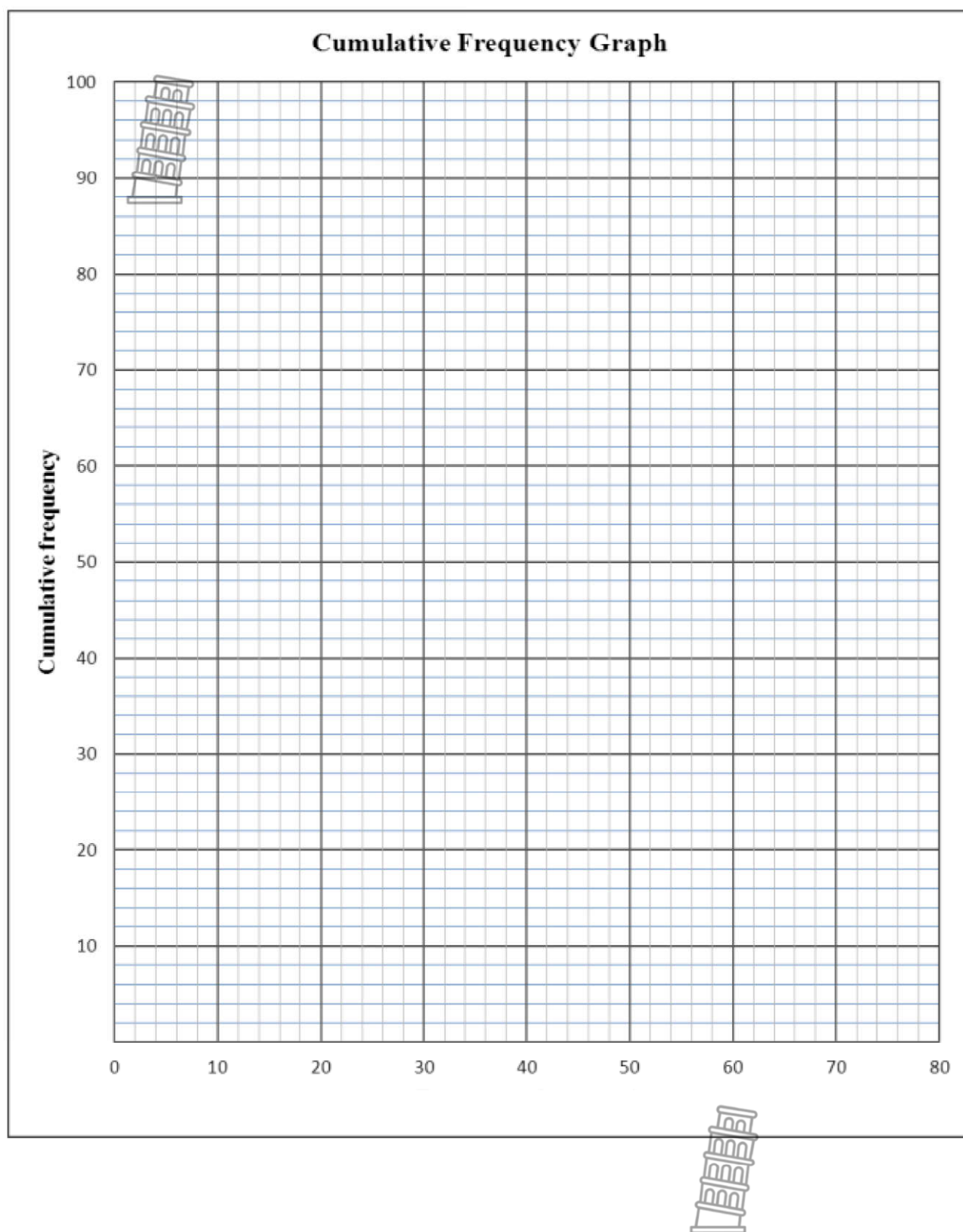
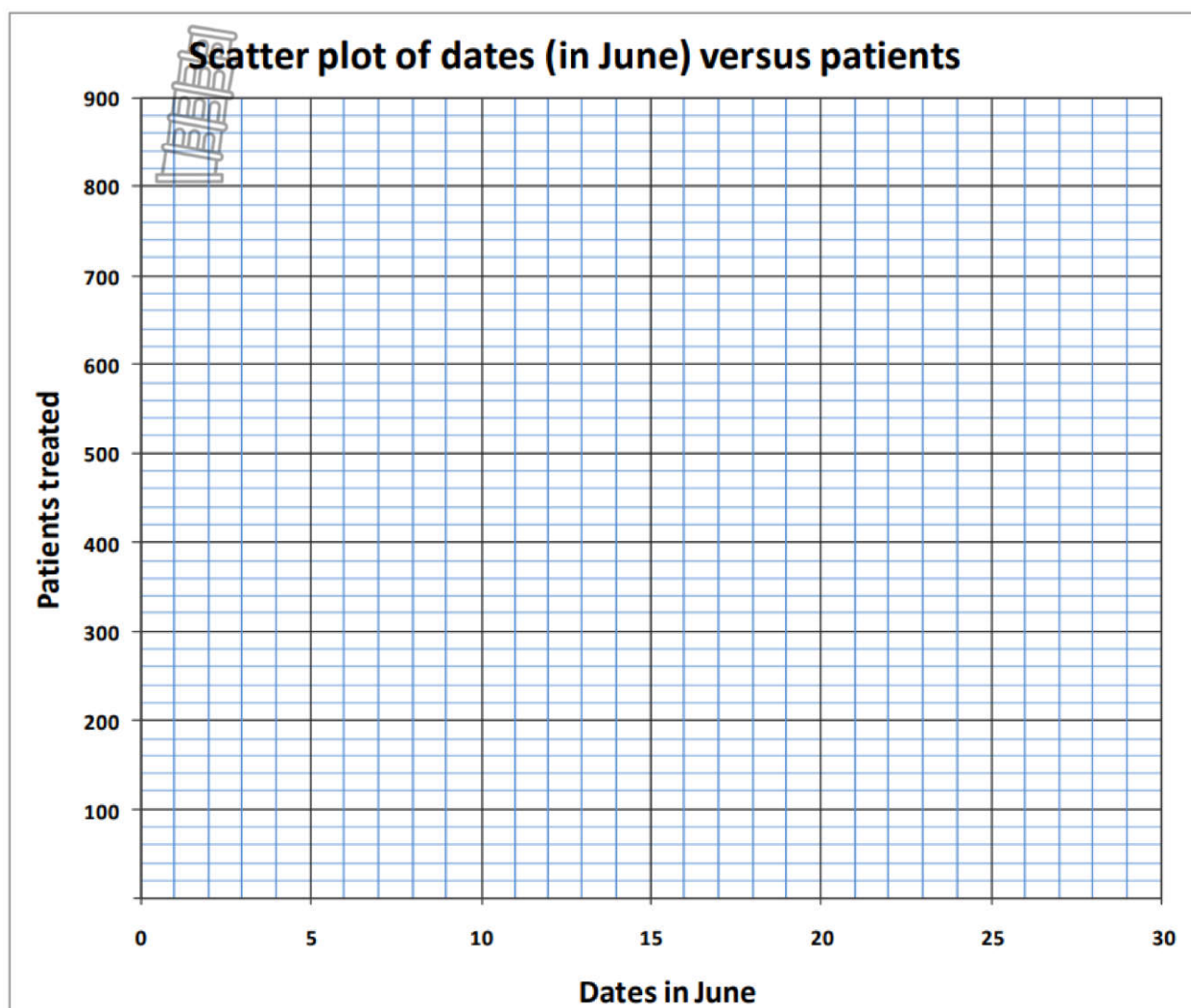
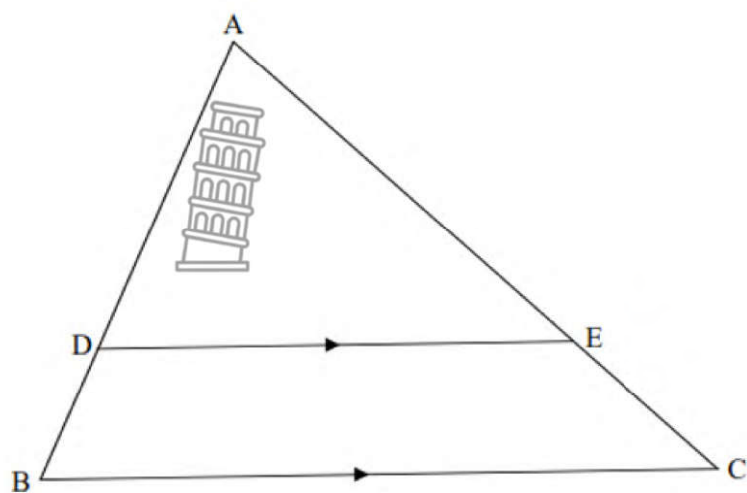


DIAGRAM SHEET 2

QUESTIONS 2.1 AND 2.4

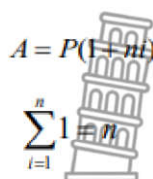


QUESTION 9.1



INFORMATION SHEET: MATHEMATICS

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$



$$A = P(1 + ni)^n$$

$$A = P(1 - ni)^n$$

$$A = P(1 - i)^n$$

$$A = P(1 + i)^n$$

$$\sum_{i=1}^n 1 = n$$

$$\sum_{i=1}^n i = \frac{n(n+1)}{2}$$

$$T_n = a + (n-1)d$$

$$S_n = \frac{n}{2}(2a + (n-1)d)$$

$$T_n = ar^{n-1}$$

$$S_n = \frac{a(r^n - 1)}{r - 1} ; \quad r \neq 1$$

$$S_\infty = \frac{a}{1 - r} ; \quad -1 < r < 1$$

$$F = \frac{x[(1+i)^n - 1]}{i}$$

$$P = \frac{x[1 - (1+i)^{-n}]}{i}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$M\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$y = mx + c$$

$$y - y_1 = m(x - x_1)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \tan \theta$$

$$(x-a)^2 + (y-b)^2 = r^2$$

$$\text{In } \triangle ABC: \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} \quad a^2 = b^2 + c^2 - 2bc \cdot \cos A \quad \text{area } \triangle ABC = \frac{1}{2} ab \cdot \sin C$$

$$\sin(\alpha + \beta) = \sin \alpha \cdot \cos \beta + \cos \alpha \cdot \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cdot \cos \beta - \cos \alpha \cdot \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cdot \cos \beta - \sin \alpha \cdot \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cdot \cos \beta + \sin \alpha \cdot \sin \beta$$

$$\cos 2\alpha = \begin{cases} \cos^2 \alpha - \sin^2 \alpha \\ 1 - 2\sin^2 \alpha \\ 2\cos^2 \alpha - 1 \end{cases}$$

$$\sin 2\alpha = 2\sin \alpha \cdot \cos \alpha$$

$$\bar{x} = \frac{\sum x}{n}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}$$

$$P(A) = \frac{n(A)}{n(S)}$$

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$\hat{y} = a + bx$$

$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$





education

Department of
Education
FREE STATE PROVINCE

GRADE 12

MATHEMATICS

MARKING GUIDELINE

MOCK EXAM

SEPTEMBER EXAM PAPER 2

18 AUGUST 2023

MARKS: 150



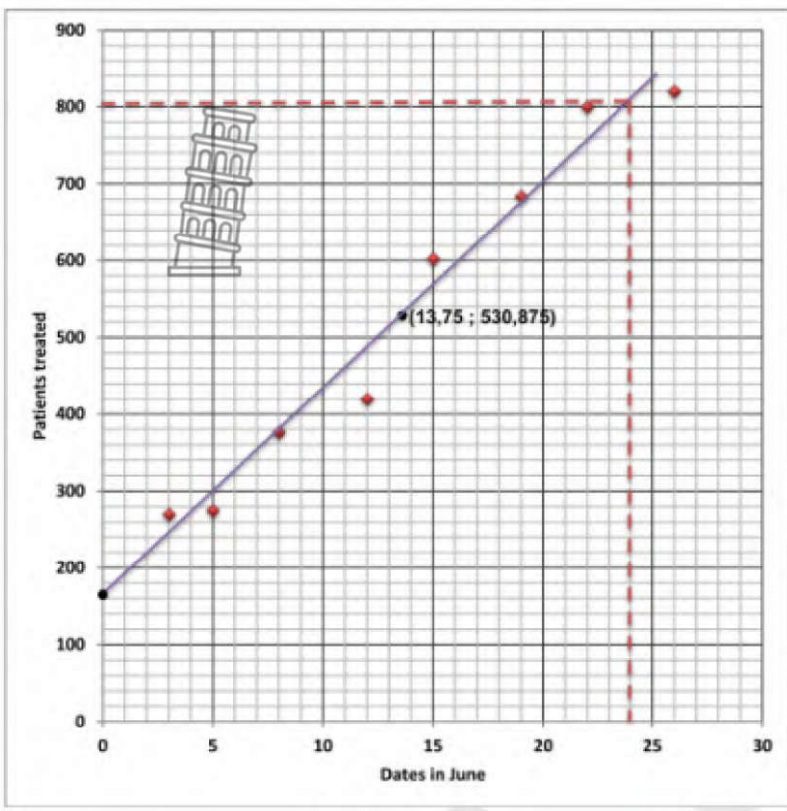

This marking guideline consists of 14 pages.

QUESTION 1

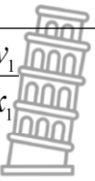

1.1	<table border="1"> <thead> <tr> <th>Speed (km/h)</th><th>Frequency (f)</th><th>Cumulative frequency</th></tr> </thead> <tbody> <tr> <td>$0 < x \leq 10$</td><td>10</td><td>10</td></tr> <tr> <td>$10 < x \leq 20$</td><td>20</td><td>30</td></tr> <tr> <td>$20 < x \leq 30$</td><td>45</td><td>75</td></tr> <tr> <td>$30 < x \leq 40$</td><td>72</td><td>147</td></tr> <tr> <td>$40 < x \leq 50$</td><td>23</td><td>170</td></tr> </tbody> </table>	Speed (km/h)	Frequency (f)	Cumulative frequency	$0 < x \leq 10$	10	10	$10 < x \leq 20$	20	30	$20 < x \leq 30$	45	75	$30 < x \leq 40$	72	147	$40 < x \leq 50$	23	170	<ul style="list-style-type: none"> ✓ column 1 values ✓ column 2 values <p>(2)</p>
Speed (km/h)	Frequency (f)	Cumulative frequency																		
$0 < x \leq 10$	10	10																		
$10 < x \leq 20$	20	30																		
$20 < x \leq 30$	45	75																		
$30 < x \leq 40$	72	147																		
$40 < x \leq 50$	23	170																		
1.2 & 1.3		<ul style="list-style-type: none"> ✓ Grounding(0; 0) ✓ Maximum (50; 170) ✓ Curve <p>(3)</p> <ul style="list-style-type: none"> ✓ Q_1 ✓ Q_2 <p>(2)</p>																		
1.4		<ul style="list-style-type: none"> ✓ Q_3 ✓ Box <p>(2)</p>																		
1.5	164 (Accept 163 – 165)	<ul style="list-style-type: none"> ✓ Answer <p>(1)</p>																		
[10]																				



QUESTION 2

2.1		<p>✓ ✓ ✓ ALL points plotted correctly</p> <p>-1 for every 2 mistakes</p> <p>-1 if points are joined</p> <p>(3)</p>
2.2	$y = 26,88x + 161,24$	<p>✓ value of $a = 161,24$</p> <p>✓ value of $b = 26,88$</p> <p>✓ equation of the line</p> <p>(3)</p>
2.3	$y = 26,88(24) + 161,24$ $y = 806,36$ 806 people treated on 24th of June	<p>✓ substitute in formula</p> <p>✓ answer as Natural Number (2)</p>
2.4	see grid	<p>✓ straight line</p> <p>✓ graph passes through (x ; y)</p> <p>✓ graph passes through y-intercept from regression line formula</p> <p>(3)</p>
2.5	$r = 0,98$ This is a very strong positive, linear correlation. As the days increase the number of patients increase	<p>✓ ✓ correct answer</p> <p>✓ interpretation</p> <p>(3)</p>
2.6	$(\bar{x} - \sigma; \bar{x} + \sigma)$ $(528,63 - 210,46; 528,63 + 210,46)$ $(318,17 ; 739,09)$ 4 patients.	 <p>✓ 318,17</p> <p>✓ (739,09)</p> <p>✓ answer</p> <p>(3)</p>

QUESTION 3

3.1	$m_{BC} = \frac{y_2 - y_1}{x_2 - x_1}$ $m_{BC} = \frac{8 - 0}{4 - 5}$ $m_{BC} = -8$ 	✓ correct substitution into the correct formula ✓ answer (2)
3.2	$AB = \sqrt{(-3 - 4)^2 + (k - 8)^2}$ $65 = 49 + k^2 - 16k + 64$ $k^2 - 16k + 48 = 0$ $(k - 4)(k - 12) = 0$ $k = 4 \text{ or } k = 12$ $k = 4$	✓ substitute A and B into distance formula ✓ standard form ✓ factors ✓ $k = 4$ (4)
3.3	$m_{BD} = \frac{8 - (-4)}{4 - (-2)}$ $m_{BD} = 2$ $m_{AC} = \frac{4 - 0}{-3 - 5} = -\frac{1}{2}$ $m_{AC} \times m_{BD} = 2 \times -\frac{1}{2} = -1$ $AC \perp BD$	✓ m_{BD} ✓ m_{AC} ✓ $m_{BD} \times m_{AC}$ (3)
3.4	$\text{midpoint of } AC = \text{midpoint of } DC$ $\frac{x + (-3)}{2} = \frac{-2 + 5}{2} \text{ and } \frac{y + 4}{2} = \frac{-4 + 0}{2}$ $x = 6 \text{ or } y = -8$ $F(6; -8)$	✓ x-coordinate ✓ y-coordinate
3.5	$m_{AD} = m_{BC} = -8$ $\tan \alpha = -8$ $\alpha = 180^\circ - \tan^{-1}(8)$ $\alpha = 97,13^\circ$ $\tan \beta = m_{BD} = 2$ $\beta = 63,43^\circ$ $O_1 = 63,43^\circ (\text{vert opp } \angle^s)$	✓ m_{AD} ✓ $\tan \alpha = -8$ ✓ $\alpha = 97,13^\circ$ ✓ $\beta = 63,43^\circ$ ✓ $\alpha + \beta$ ✓ answer  (6)

	$\hat{E}DO = \alpha - \beta$ $\hat{E}DO = 97,13^\circ - 63,43^\circ = 33,7^\circ$	
3.6	$AC = \sqrt{(5 - (-3))^2 + (0 - 4)^2} = \sqrt{80} = 4\sqrt{5}$ $DP = \sqrt{(-2 - 1)^2 + (-4 - 2)^2} = \sqrt{45} = 3\sqrt{5}$ $\text{Area of } \triangle ADC = \frac{1}{2} AC \times DP$ $\text{Area of } \triangle ADC = \frac{1}{2} (4\sqrt{5})(4\sqrt{5})$ $\text{Area of } \triangle ADC = 30 \text{ square units}$	✓ length of AC ✓ length of DP ✓ correct substitution into formula ✓ answer (4)
		[08]


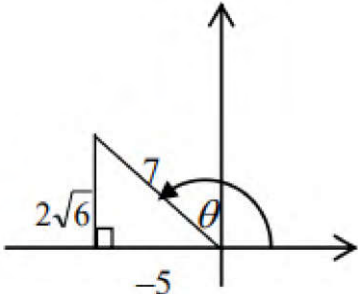
QUESTION 4

4		
4.1	$OB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $OB = \sqrt{(-4 - 0)^2 + (-6 - 0)^2}$ $OB = \sqrt{52}$ $OB = 2\sqrt{13}$ $r = \sqrt{13}$	✓ substitution ✓ $OB = \sqrt{52}$ ✓ $r = \sqrt{13}$ (3)
4.2	$C\left(\frac{-4+0}{2}; \frac{-6+0}{2}\right)$ $C(-2; -3)$ $(x+2)^2 + (y+3)^2 = 13$	
4.3	Right-angled triangle, tangent perpendicular to the radius.	✓ right angled \triangle ✓ reason (2)
4.4	$m_{OB} = \frac{y_2 - y_1}{x_2 - x_1}$ $m_{BO} = \frac{-6 - 0}{-4 - 0}$ $m_{BO} = \frac{3}{2}$ $m_{KL} = -\frac{2}{3}$ $y - y_1 = m(x - x_1)$ $y + 6 = -\frac{2}{3}(x + 4)$	✓ m_{OB} ✓ m_{KL} ✓ substitution ✓ answer (4)

	$y = -\frac{2}{3}x - \frac{26}{3}$	
4.5	E(0;-6)	✓✓ answer (2)
4.6	$(x+2)^2 + (0+3)^2 = 13$ $F(-4;0)$ $m_{FC} = \frac{-3-0}{-2+4} = -\frac{3}{2}$ $m_{CE} = \frac{-3+6}{-2+0} = -\frac{3}{2}$ Points F, C and E are collinear EF is a diameter	✓ x_F ✓ y_F ✓ m_{FC} ✓ m_{CE} ✓ Points F, C and E are collinear (5)
		[20]


QUESTION 5

5.1.1	$\tan 58^\circ = m$ $x^2 + y^2 = r^2$ $1^2 + m^2 = r^2$ $\sqrt{1+m^2} = r$ $\sin 58^\circ = \frac{m}{\sqrt{1+m^2}}$	$\checkmark \sqrt{1+m^2} = r$ \checkmark answer (2)
5.1.2	$\sin 296^\circ = -\sin 64^\circ$ $\sin 296^\circ = -\sin 2(32^\circ)$ $\sin 296^\circ = -2 \sin 32^\circ \times \cos 32^\circ$ $\sin 296^\circ = -2 \times \frac{m}{\sqrt{1+m^2}} \times \frac{1}{\sqrt{1+m^2}}$ $\sin 296^\circ = -\frac{2m}{1+m^2}$	$\checkmark -\sin 64^\circ$ \checkmark substitution \checkmark answer (3)
5.2.1	$5 \tan \theta + 2\sqrt{6} = 0$	

	 $\tan \theta = -\frac{2\sqrt{6}}{5}$ $r^2 = y^2 + x^2$ $r^2 = (-2\sqrt{6})^2 + (5)^2$ $r^2 = 49$ $r = 7$ $\sin \theta = \frac{2\sqrt{6}}{7}$	 $0^\circ < \theta < 270^\circ$	$\checkmark r = \frac{\sqrt{649}}{5}$ $\checkmark \sin \theta = \frac{2\sqrt{6}}{\frac{\sqrt{649}}{5}}$ <p>(2)</p>
5.2.2	$\cos \theta = -\frac{5}{7}$	\checkmark answer (1)	
5.2.3	$\frac{14 \cos \theta + 7\sqrt{6} \sin \theta}{\cos(-240^\circ) \tan 225^\circ}$ $= \frac{14\left(-\frac{5}{7}\right) + 7\sqrt{6}\left(\frac{2\sqrt{6}}{7}\right)}{\cos(90^\circ + 30^\circ) \tan(180^\circ + 45^\circ)}$ $= \frac{-10 + 12}{-\sin 30^\circ \cdot \tan 45^\circ}$ $= \frac{2}{-\frac{1}{2} \times 1}$ $= -4$	$\checkmark -\sin 30^\circ$ $\checkmark \tan 45^\circ$ $\checkmark -\frac{1}{2} \times 1$ $\checkmark \text{ answer}$ <p>(4)</p>	
			[15]

QUESTION 6

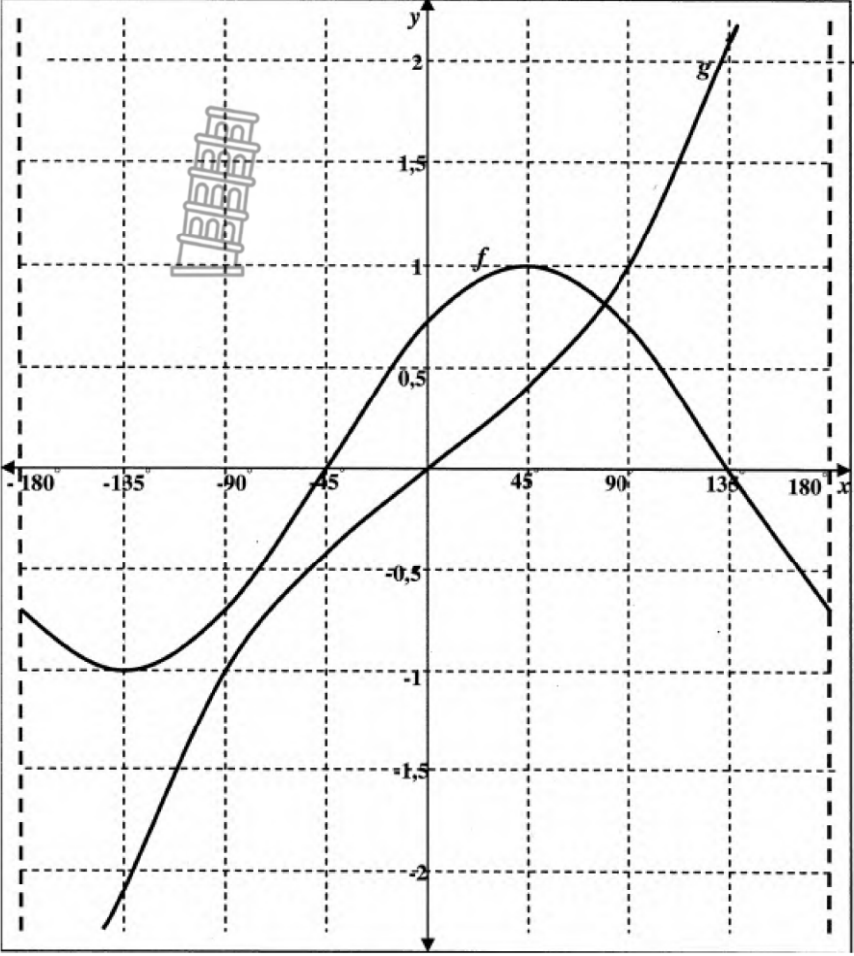


6.1	$\frac{\cos(180^\circ + x) \cdot \tan(360^\circ - x) \cdot \sin^2(90^\circ - x)}{\sin(180^\circ - x)} + \sin^2 x$ $= \frac{(-\cos x) \cdot (-\tan x) \cdot \cos^2 x}{\sin x} + \sin^2 x$ $= \frac{\cos x \cdot \frac{\sin x}{\cos x} \cdot \cos^2 x}{\sin x} + \sin^2 x$ $= \cos^2 x + \sin^2 x$ $= 1$	<ul style="list-style-type: none"> ✓ $-\cos x$ ✓ $-\tan x$ ✓ $\cos^2 x$ ✓ $\sin x$ ✓ $\cos^2 x + \sin^2 x$ ✓ answer <p style="text-align: right;">(6)</p>
6.2.1	$\cos(A - B) - \cos(A + B)$ $= \cos A \cos B + \sin A \sin B - [\cos A \cos B - \sin A \sin B]$ $= \cos A \cos B + \sin A \sin B - \cos A \cos B + \sin A \sin B$ $= 2\sin A \sin B$	<ul style="list-style-type: none"> ✓ ✓ ✓ <p style="text-align: right;">(3)</p>
6.2.2	$\cos 15^\circ - \cos 75^\circ = \cos(45^\circ - 30^\circ) - \cos(45^\circ + 30^\circ)$ $= 2\sin 45^\circ \cdot \sin 30^\circ$ $= 2 \times \frac{\sqrt{2}}{2} \times \frac{1}{2} \quad \text{or/ of} \quad 2 \times \frac{1}{\sqrt{2}} \times \frac{1}{2}$ $= \frac{\sqrt{2}}{2} \quad \text{or/ of} \quad \frac{1}{\sqrt{2}}$ <p>OR</p> $\cos 15^\circ - \cos 75^\circ$ $= \cos(45^\circ - 30^\circ) - \cos(45^\circ + 30^\circ)$ $= \cos 45^\circ \cos 30^\circ + \sin 45^\circ \sin 30^\circ - [\cos 45^\circ \cos 30^\circ - \sin 45^\circ \sin 30^\circ]$ $= 2\sin 45^\circ \sin 30^\circ$ $= 2 \times \frac{\sqrt{2}}{2} \times \frac{1}{2} \quad \text{or/ of} \quad 2 \times \frac{1}{\sqrt{2}} \times \frac{1}{2}$ $= \frac{\sqrt{2}}{2} \quad \text{or/ of} \quad \frac{1}{\sqrt{2}}$ 	<ul style="list-style-type: none"> ✓ ✓ ✓ ✓ <p style="text-align: right;">(4)</p>

6.3	$AB^2 = (\cos \theta - 6)^2 + (\sin \theta - 7)^2$ $86 = \cos^2 \theta - 12 \cos \theta + 36 + \sin^2 \theta - 14 \sin \theta + 49$ $86 = 1 + 36 + 49 - 12 \cos \theta - 14 \sin \theta$ $0 = -12 \cos \theta - 14 \sin \theta$ $14 \sin \theta = -12 \cos \theta$ $\frac{\sin \theta}{\cos \theta} = \frac{-12}{14}$ $\tan \theta = -\frac{6}{7} / -0,86$	<div style="text-align: center;"> ✓ ✓ ✓ ✓ </div> <div style="text-align: right;">(4)</div>
-----	--	---

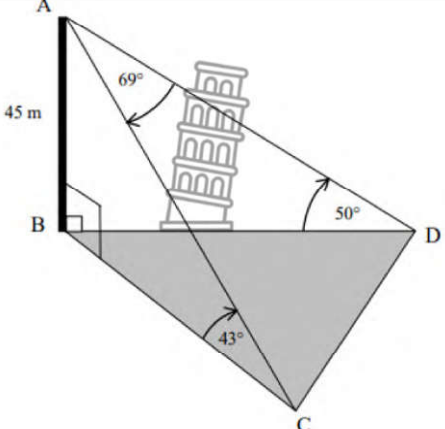


QUESTION 7

7.1		<ul style="list-style-type: none"> ✓ shape f ✓ intercepts ✓ turning point ✓ shape f ✓ intercepts ✓ turning point <p style="text-align: right;">(6)</p>
7.2.1	$x = -45^\circ$ or $x = 135^\circ$	✓ ✓ answer (2)
7.2.2	$x = 180^\circ$ or/ of $x = -180^\circ$	✓ ✓ answer (2)
7.2.3	$y \in [-1; 1]$ or/ of $-1 \leq y \leq 1$	✓ answer (1)
7.2.4	1	✓ answer (1)
7.2.5	$x \in (-180^\circ; -45^\circ)$ or/ of $(0^\circ; 135^\circ)$ OR $-180^\circ < x < -45^\circ$ or/ of $0^\circ < x < 135^\circ$	<ul style="list-style-type: none"> ✓ end points ✓ notation ✓ answer <p>(3)</p>
[15]		



QUESTION 7

		
7.1	$\sin 43^\circ = \frac{45}{AC}$ $AC = 66m$ $\sin 43^\circ = \frac{45}{AC}$ $\sin 50^\circ = \frac{45}{AD}$ $AD = 58,74m$	$\checkmark \sin 43^\circ = \frac{45}{AC}$ $\checkmark AC$ $\checkmark \sin 43^\circ = \frac{45}{AC}$ $\checkmark AD$ <div style="text-align: right;">(4)</div>
7.2	$CD^2 = AC^2 + AD^2 - 2AC \cdot AD \cos 69^\circ$ $CD^2 = (66)^2 + (58.74)^2 - 2(66)(58.74)\cos 69^\circ$ $CD^2 = 5027,72$ $CD = 70.91m$	\checkmark using cosine rule \checkmark substitution \checkmark answer <div style="text-align: right;">(3)</div>

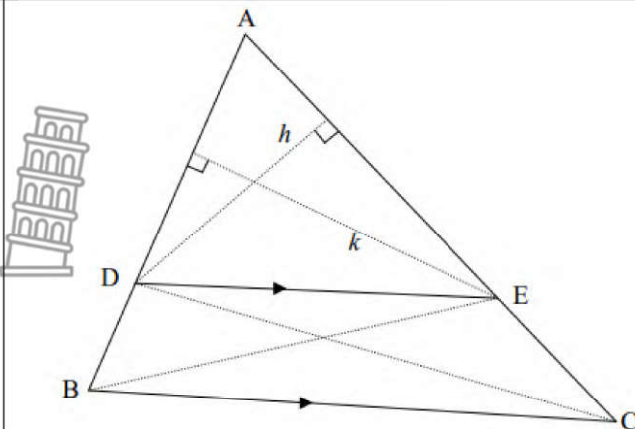



QUESTION 8

8.1.1	$\hat{D}_1 = \hat{B}_2 = 30^\circ$ (alter angles DC parallel GB)	✓ S&R (1)
8.1.2	$\hat{B}_1 = \hat{C}_1 = 60^\circ$ (tan-chord theorem)	✓ S ✓ R (2)
8.1.3	$\hat{C}_2 = 90^\circ$ (sum of angles in triangle)	✓ S&R (1)
8.1.4	$\hat{DAB} + \hat{C}_2 = 180^\circ$ $\hat{DAB} = 90^\circ$	✓ S ✓ R (2)
8.2	Yes is diameter, converse angle in a semi-circle	✓ S ✓ R (2)



QUESTION 9

9.1	 <p>Construction: Connect DC and BE and draw the altitudes k and h</p> $\frac{\text{Area } \triangle ADE}{\text{Area } \triangle BDE} = \frac{\frac{1}{2} \times AD \times k}{\frac{1}{2} \times BD \times k} = \frac{AD}{BD}$ $\frac{\text{Area } \triangle ADE}{\text{Area } \triangle DEC} = \frac{\frac{1}{2} \times AE \times h}{\frac{1}{2} \times EC \times h} = \frac{AE}{EC}$ <p>but/maar: Area $\triangle BDE$ = Area $\triangle DEC$ [DE common base and DE \parallel BC/ DE gemeensk basis en DE \parallel BC]</p> $\therefore \frac{\text{Area } \triangle ADE}{\text{Area } \triangle BDE} = \frac{\text{Area } \triangle ADE}{\text{Area } \triangle DEC}$ $\therefore \frac{AD}{BD} = \frac{AE}{EC}$	<p>✓ constr</p> <p>✓ S</p> <p>✓ S</p> <p>✓ S ✓ R</p> <p>✓ conclusion</p> <p>(6)</p>
9.2.1	tangent-chord theorem	✓ R (1)
9.2.2	<p>In $\triangle ABC$ and $\triangle ADB$:</p> <p>$\hat{A}_1 = \hat{A}_1$ [common/gemeenskaplik]</p> <p>$\hat{B}_1 = \hat{D}_1$ [proven/bewys in 10.2.1]</p> <p>$\therefore \triangle ABC \parallel \triangle ADB$ [\angle; \angle; \angle]</p> <p>OR</p> <p>In $\triangle ABC$ and $\triangle ADB$:</p> <p>$\hat{A}_1 = \hat{A}_1$ [common/gemeenskaplik]</p> <p>$\hat{B}_1 = \hat{D}_1$ [proven/bewys in 10.2.1]</p> <p>$\hat{B}_1\hat{C}\hat{A} = \hat{B}_2$ [\angles of $\Delta = 180^\circ$]</p> <p>$\therefore \triangle ABC \parallel \triangle ADB$</p>	<p>✓ S</p> <p>✓ S</p> <p>✓ R</p> <p>✓ S</p> <p>✓ S</p> <p>✓ R</p>
9.2.3	<p>$\hat{E}_2 = \hat{F}_1$ [verwiss \anglee/alternate \angles ; EA \parallel GF]</p> <p>$\hat{F}_1 = \hat{D}_2$ [ext \angle of cyc quad DGFC/buite \angle v kdvh DGFC]</p> <p>$\therefore \hat{E}_2 = \hat{D}_2$</p> 	<p>✓ S ✓ R</p> <p>✓ S ✓ R</p>

9.2.4	<p>In $\triangle AEC$ and $\triangle ADE$:</p> <p>$\hat{A}_2 = \hat{A}_2$ [common/gemeenskaplik]</p> <p>$\hat{E}_2 = \hat{D}_2$ [proven/bewys in 10.2.3]</p> <p>$\therefore \triangle AEC \parallel \triangle ADE$ [\angle; \angle; \angle]</p> <p>$\frac{AE}{AD} = \frac{AC}{AE}$</p> <p>$AE^2 = AD \times AC$</p> <p>OR</p> <p>In $\triangle AEC$ and $\triangle ADE$:</p> <p>$\hat{A}_2 = \hat{A}_2$ [common/gemeenskaplik]</p> <p>$\hat{E}_2 = \hat{D}_2$ [proven/bewys in 10.2.3]</p> <p>$\hat{ACE} = \hat{G}_1$ [\angles of $\Delta = 180^\circ$ OR ext \angle of cyc quad DGFC/ buite \angle v kdvh DGFC]</p> <p>$\therefore \triangle AEC \parallel \triangle ADE$</p> <p>$\therefore \frac{AE}{AD} = \frac{AC}{AE}$</p> <p>$\therefore AE^2 = AD \times AC$</p>	<p>✓ S</p> <p>✓ S</p> <p>✓ R</p> <p>✓ S</p> <p>✓ S</p> <p>✓ S</p> <p>✓ R</p> <p>✓ S</p>
9.2.5	<p>$\frac{AB}{AD} = \frac{AC}{AB}$ [$\triangle ABC \parallel \triangle ADB$]</p> <p>$AB^2 = AD \times AC$</p> <p>$= AE^2$ [from 10.2.4]</p> <p>$\therefore AB = AE$</p>	<p>✓ S</p> <p>✓ S</p> <p>✓ S</p>
		[21]

